## Package 'bestNormalize'

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Type Package

**Title** Normalizing Transformation Functions

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Description Estimate a suite of normalizing transformations, including a new adaptation of a technique based on ranks which can guarantee normally distributed transformed data if there are no ties: ordered quantile normalization (ORQ). ORQ normalization combines a rank-mapping approach with a shifted logit approximation that allows the transformation to work on data outside the original domain. It is also able to handle new data within the original domain via linear interpolation. The package is built to estimate the best normalizing transformation for a vector consistently and accurately. It implements the Box-Cox transformation, the Yeo-Johnson transformation, three types of Lambert WxF transformations, and the ordered quantile normalization transformation. It estimates the normalization efficacy of other commonly used transformations, and it allows users to specify custom transformations or normalization statistics. Finally, functionality can be integrated into a machine learning workflow via recipes.

URL https://petersonr.github.io/bestNormalize/,
 https://github.com/petersonR/bestNormalize

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## NeedsCompilation no

Author Ryan A Peterson [aut, cre] (ORCID:

<https://orcid.org/0000-0002-4650-5798>)

Maintainer Ryan A Peterson < ryan-peterson@uiowa.edu>

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 $bestNormalize-package \quad bestNormalize: \ Flexibly \ calculate \ the \ best \ normalizing \ transformation \\ for \ a \ vector$ 

## Description

The bestNormalize package provides several normalizing transformations, and introduces a new transformation based off of the order statistics, orderNorm. Perhaps the most useful function is bestNormalize, which attempts all of these transformations and picks the best one based off of a goodness of fit statistic.

## Author(s)

Maintainer: Ryan A Peterson < ryan-peterson@uiowa.edu > (ORCID)

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## See Also

Useful links:

```
• https://petersonr.github.io/bestNormalize/
```

• https://github.com/petersonR/bestNormalize

arcsinh\_x

arcsinh(x) Transformation

## **Description**

Perform a arcsinh(x) transformation

## Usage

```
arcsinh_x(x, standardize = TRUE, ...)
## S3 method for class 'arcsinh_x'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'arcsinh_x'
print(x, ...)
```

## **Arguments**

x A vector to normalize with with x

transformation attempts a standard normal

... additional arguments

object an object of class 'arcsinh\_x'

newdata a vector of data to be (potentially reverse) transformed

inverse if TRUE, performs reverse transformation

#### **Details**

arcsinh\_x performs an arcsinh transformation in the context of bestNormalize, such that it creates a transformation that can be estimated and applied to new data via the predict function.

The function is explicitly:  $log(x + sqrt(x^2 + 1))$ 

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## Value

A list of class arcsinh\_x with elements

x.t transformed original data

x original data

mean mean after transformation but prior to standardization sd after transformation but prior to standardization

n number of nonmissing observations norm\_stat Pearson's P / degrees of freedom standardize was the transformation standardized

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

## **Examples**

```
x <- rgamma(100, 1, 1)
arcsinh_x_obj <- arcsinh_x(x)
arcsinh_x_obj
p <- predict(arcsinh_x_obj)
x2 <- predict(arcsinh_x_obj, newdata = p, inverse = TRUE)
all.equal(x2, x)</pre>
```

autotrader

Prices of 6,283 cars listed on Autotrader

## **Description**

A dataset containing the prices and other attributes of over 6000 cars in the Minneapolis area.

## Usage

autotrader

#### **Format**

A data frame with 6283 rows and 10 variables:

price price, in US dollars

Car\_Info Raw description from website

Link hyperlink to listing (must be appended to https://www.autotrader.com/)

Make Car manufacturer

Year Year car manufactured

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```
Location Location of listing

Radius Radius chosen for search

mileage mileage on vehicle

status used/new/certified

model make and model, separated by space
```

## **Source**

```
https://www.autotrader.com/
```

bestLogConstant	Calculate and perform best normalizing log transformation (experi-
	mental)

## Description

Similar to bestNormalize, this selects the best candidate constant for a log transformation on the basis of the Pearson P test statistic for normality. The transformation that has the lowest P (calculated on the transformed data) is selected. This function is currently in development and may not behave as expected.

See details for more information.

### Usage

```
bestLogConstant(x, a, standardize = TRUE, ...)
## S3 method for class 'bestLogConstant'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'bestLogConstant'
print(x, ...)
```

## Arguments

inverse

x	A vector to normalize
а	(optional) a list of candidate constants to choose from
standardize	If TRUE, the transformed values are also centered and scaled, such that the transformation attempts a standard normal. This will not change the normality statistic.
	additional arguments.
object	an object of class 'bestLogConstant'
newdata	a vector of data to be (reverse) transformed

if TRUE, performs reverse transformation

## **Details**

bestLogConstant estimates the optimal normalizing constant for a log transformation. This transformation can be performed on new data, and inverted, via the predict function.

#### Value

A list of class bestLogConstant with elements

```
x.t transformed original data

x original data

norm_stats Pearson's Pearson's P/degrees of freedom

method out-of-sample or in-sample, number of folds + repeats

chosen_constant

the chosen constant transformation (of class 'log_x')

other_transforms

the other transformations (of class 'log_x')
```

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

## See Also

```
bestNormalize, log_x,
```

bestNormalize

Calculate and perform best normalizing transformation

## **Description**

Performs a suite of normalizing transformations, and selects the best one on the basis of the Pearson P test statistic for normality. The transformation that has the lowest P (calculated on the transformed data) is selected. See details for more information.

## Usage

```
bestNormalize(
    x,
    standardize = TRUE,
    allow_orderNorm = TRUE,
    allow_lambert_s = FALSE,
    allow_lambert_h = FALSE,
    allow_exp = TRUE,
    out_of_sample = TRUE,
    cluster = NULL,
    k = 10,
    r = 5,
```

```
loo = FALSE,
      warn = FALSE,
      quiet = FALSE,
      tr_opts = list(),
      new_transforms = list(),
      norm_stat_fn = NULL,
    )
    ## S3 method for class 'bestNormalize'
    predict(object, newdata = NULL, inverse = FALSE, ...)
    ## S3 method for class 'bestNormalize'
    print(x, ...)
    ## S3 method for class 'bestNormalize'
    tidy(x, ...)
Arguments
                      A 'bestNormalize' object.
    Χ
                      If TRUE, the transformed values are also centered and scaled, such that the
    standardize
                      transformation attempts a standard normal. This will not change the normality
                      statistic.
    allow_orderNorm
                      set to FALSE if orderNorm should not be applied
    allow_lambert_s
                      Set to FALSE if the lambertW of type "s" should not be applied (see details).
                      Expect about 2-3x elapsed computing time if TRUE.
    allow_lambert_h
                      Set to TRUE if the lambertW of type "h" and "hh" should be applied (see de-
                      tails). Expect about 2-4x elapsed computing time.
    allow_exp
                      Set to TRUE if the exponential transformation should be applied (sometimes
                      this will cause errors with heavy right skew)
    out_of_sample
                     if FALSE, estimates quickly in-sample performance
    cluster
                      name of cluster set using makeCluster
    k
                      number of folds
                      number of repeats
                      should leave-one-out CV be used instead of repeated CV? (see details)
    100
                      Should bestNormalize warn when a method doesn't work?
    warn
                      Should a progress-bar not be displayed for cross-validation progress?
    quiet
    tr_opts
                      a list (of lists), specifying options to be passed to each transformation (see de-
                     a named list of new transformation functions and their predict methods (see
    new_transforms
                      details)
```

norm\_stat\_fn if specified, a function to calculate to assess normality (default is the Pearson

chi-squared statistic divided by its d.f.)

... not used

object an object of class 'bestNormalize'

newdata a vector of data to be (reverse) transformed inverse if TRUE, performs reverse transformation

#### **Details**

bestNormalize estimates the optimal normalizing transformation. This transformation can be performed on new data, and inverted, via the predict function.

This function currently estimates the Yeo-Johnson transformation, the Box Cox transformation (if the data is positive), the  $log_10(x+a)$  transformation, the square-root (x+a) transformation, and the arcsinh transformation. a is set to max(0, -min(x) + eps) by default. If allow\_orderNorm == TRUE and if out\_of\_sample == FALSE then the ordered quantile normalization technique will likely be chosen since it essentially forces the data to follow a normal distribution. More information on the orderNorm technique can be found in the package vignette, or using ?orderNorm.

Repeated cross-validation is used by default to estimate the out-of-sample performance of each transformation if out\_of\_sample = TRUE. While this can take some time, users can speed it up by creating a cluster via the parallel package's makeCluster function, and passing the name of this cluster to bestNormalize via the cl argument. For best performance, we recommend the number of clusters to be set to the number of repeats r. Care should be taken to account for the number of observations per fold; too small a number and the estimated normality statistic could be inaccurate, or at least suffer from high variability.

As of version 1.3, users can use leave-one-out cross-validation as well for each method by setting loo to TRUE. This will take a lot of time for bigger vectors, but it will have the most accurate estimate of normalization efficacy. Note that if this method is selected, arguments k, r are ignored. This method will still work in parallel with the cl argument.

Note that the Lambert transformation of type "h" or "hh" can be done by setting allow\_lambert\_h = TRUE, however this can take significantly longer to run.

Use tr\_opts in order to set options for each transformation. For instance, if you want to overide the default a selection for  $\log_x$ , set tr\_opts $\log_x = \text{list}(a = 1)$ .

See the package's vignette on how to use custom functions with bestNormalize. All it takes is to create an S3 class and predict method for the new transformation and load it into the environment, then the new custom function (and its predict method) can be passed to bestNormalize with new\_transform.

#### Value

A list of class bestNormalize with elements

x.t transformed original data

x original data

norm\_stats Pearson's Pearson's P / degrees of freedom

method out-of-sample or in-sample, number of folds + repeats

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

## See Also

boxcox, orderNorm, yeojohnson

## **Examples**

```
x < - rgamma(100, 1, 1)
## Not run:
# With Repeated CV
BN_obj <- bestNormalize(x)
BN_obj
p <- predict(BN_obj)</pre>
x2 <- predict(BN_obj, newdata = p, inverse = TRUE)</pre>
all.equal(x2, x)
## End(Not run)
## Not run:
# With leave-one-out CV
BN_obj <- bestNormalize(x, loo = TRUE)
BN_obj
p <- predict(BN_obj)</pre>
x2 <- predict(BN_obj, newdata = p, inverse = TRUE)</pre>
all.equal(x2, x)
## End(Not run)
# Without CV
BN_obj <- bestNormalize(x, allow_orderNorm = FALSE, out_of_sample = FALSE)
BN_obj
p <- predict(BN_obj)</pre>
x2 <- predict(BN_obj, newdata = p, inverse = TRUE)</pre>
all.equal(x2, x)
```

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## **Description**

This function will perform a binarizing transformation, which could be used as a last resort if the data cannot be adequately normalized. This may be useful when accidentally attempting normalization of a binary vector (which could occur if implementing bestNormalize in an automated fashion).

Note that the transformation is not one-to-one, in contrast to the other functions in this package.

#### Usage

```
binarize(x, location_measure = "median")
## S3 method for class 'binarize'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'binarize'
print(x, ...)
```

## **Arguments**

x A vector to binarize

location\_measure

which location measure should be used? can either be "median", "mean", "mode",

a number, or a function.

object an object of class 'binarize'

newdata a vector of data to be (reverse) transformed inverse if TRUE, performs reverse transformation

... additional arguments

## Value

A list of class binarize with elements

x.t transformed original data

x original data

method location\_measure used for original fitting

location estimated location\_measure

n number of nonmissing observations norm\_stat Pearson's P / degrees of freedom

The predict function with inverse = FALSE returns the numeric value (0 or 1) of the transformation on newdata (which defaults to the original data).

If inverse = TRUE, since the transform is not 1-1, it will create and return a factor that indicates where the original data was cut.

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## **Examples**

```
x <- rgamma(100, 1, 1)
binarize_obj <- binarize(x)
(p <- predict(binarize_obj))
predict(binarize_obj, newdata = p, inverse = TRUE)</pre>
```

boxcox

**Box-Cox Normalization** 

## **Description**

Perform a Box-Cox transformation and center/scale a vector to attempt normalization

## Usage

```
boxcox(x, standardize = TRUE, ...)
## S3 method for class 'boxcox'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'boxcox'
print(x, ...)
```

## **Arguments**

X	A vector to normalize with Box-Cox
standardize	If TRUE, the transformed values are also centered and scaled, such that the transformation attempts a standard normal
	Additional arguments that can be passed to the estimation of the lambda parameter (lower, upper, epsilon)
object	an object of class 'boxcox'
newdata	a vector of data to be (reverse) transformed
inverse	if TRUE, performs reverse transformation

## **Details**

boxcox estimates the optimal value of lambda for the Box-Cox transformation. This transformation can be performed on new data, and inverted, via the predict function.

The function will return an error if a user attempt to transform nonpositive data.

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## Value

A list of class boxcox with elements

x.t transformed original data

x original data

mean mean after transformation but prior to standardization
sd sd after transformation but prior to standardization
lambda estimated lambda value for skew transformation

n number of nonmissing observations norm\_stat Pearson's P / degrees of freedom standardize was the transformation standardized

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

#### References

Box, G. E. P. and Cox, D. R. (1964) An analysis of transformations. Journal of the Royal Statistical Society B, 26, 211-252.

## See Also

boxcox

## **Examples**

```
x <- rgamma(100, 1, 1)
bc_obj <- boxcox(x)
bc_obj
p <- predict(bc_obj)
x2 <- predict(bc_obj, newdata = p, inverse = TRUE)
all.equal(x2, x)</pre>
```

double\_reverse\_log

Double Reverse Log(x + a) Transformation

## Description

First reverses scores, then perform a  $log\_b(x)$  normalization transformation, and then reverses scores again.

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## Usage

```
double_reverse_log(
    x,
    b = 10,
    standardize = TRUE,
    eps = diff(range(x, na.rm = TRUE))/10,
    warn = TRUE,
    ...
)

## S3 method for class 'double_reverse_log'
predict(object, newdata = NULL, inverse = FALSE, ...)

## S3 method for class 'double_reverse_log'
print(x, ...)
```

#### **Arguments**

x A vector to normalize with with x b The base of the log (defaults to 10)

standardize If TRUE, the transformed values are also centered and scaled, such that the

transformation attempts a standard normal

eps The cushion for the transformation range (defaults to 10 percent)

warn Should a warning result from infinite values?

... additional arguments

object an object of class 'double\_reverse\_log'

newdata a vector of data to be (potentially reverse) transformed

inverse if TRUE, performs reverse transformation

#### **Details**

double\_reverse\_log performs a simple log transformation in the context of bestNormalize, such that it creates a transformation that can be estimated and applied to new data via the predict function. The parameter a is essentially estimated by the training set by default (estimated as the minimum possible to some extent epsilon), while the base must be specified beforehand.

#### Value

A list of class double\_reverse\_log with elements

x.t transformed original data

x original data

mean mean after transformation but prior to standardization sd after transformation but prior to standardization

b estimated base b value

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n number of nonmissing observations norm\_stat Pearson's P / degrees of freedom standardize was the transformation standardized

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

## **Examples**

```
x <- rgamma(100, 1, 1)
double_reverse_log_obj <- double_reverse_log(x)
double_reverse_log_obj
p <- predict(double_reverse_log_obj)
x2 <- predict(double_reverse_log_obj, newdata = p, inverse = TRUE)
all.equal(x2, x)</pre>
```

exp\_x

exp(x) Transformation

## **Description**

Perform a exp(x) transformation

## Usage

```
exp_x(x, standardize = TRUE, warn = TRUE, ...)
## S3 method for class 'exp_x'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'exp_x'
print(x, ...)
```

## **Arguments**

X	A vector to normalize with with x
standardize	If TRUE, the transformed values are also centered and scaled, such that the transformation attempts a standard normal
warn	Should a warning result from infinite values?
	additional arguments
object	an object of class 'exp_x'
newdata	a vector of data to be (potentially reverse) transformed
inverse	if TRUE, performs reverse transformation

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#### **Details**

exp\_x performs a simple exponential transformation in the context of bestNormalize, such that it creates a transformation that can be estimated and applied to new data via the predict function.

#### Value

A list of class exp\_x with elements

x.t transformed original data
x original data
mean after transformation but prior to standardization
sd sd after transformation but prior to standardization
n number of nonmissing observations
norm\_stat Pearson's P / degrees of freedom

was the transformation standardized

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

## **Examples**

standardize

```
x <- rgamma(100, 1, 1)
exp_x_obj <- exp_x(x)
exp_x_obj
p <- predict(exp_x_obj)
x2 <- predict(exp_x_obj, newdata = p, inverse = TRUE)
all.equal(x2, x)</pre>
```

lambert

Lambert W x F Normalization

## **Description**

Perform Lambert's W x F transformation and center/scale a vector to attempt normalization via the LambertW package.

## Usage

```
lambert(x, type = "s", standardize = TRUE, warn = FALSE, ...)
## S3 method for class 'lambert'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'lambert'
print(x, ...)
```

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## Arguments

x A vector to normalize with Box-Cox

type a character indicating which transformation to perform (options are "s", "h", and

"hh", see details)

transformation attempts a standard normal

warn should the function show warnings

... Additional arguments that can be passed to the LambertW::Gaussianize function

object an object of class 'lambert'

newdata a vector of data to be (reverse) transformed inverse if TRUE, performs reverse transformation

#### **Details**

lambert uses the LambertW package to estimate a normalizing (or "Gaussianizing") transformation. This transformation can be performed on new data, and inverted, via the predict function.

NOTE: The type = "s" argument is the only one that does the 1-1 transform consistently, and so it is the only method currently used in bestNormalize(). Use type = "h" or type = 'hh' at risk of not having this estimate 1-1 transform. These alternative types are effective when the data has exceptionally heavy tails, e.g. the Cauchy distribution.

Additionally, sometimes (depending on the distribution) this method will be unable to extrapolate beyond the observed bounds. In these cases, NaN is returned.

#### Value

A list of class lambert with elements

x.t transformed original data

x original data

mean after transformation but prior to standardization

sd sd after transformation but prior to standardization

tau.mat estimated parameters of LambertW::Gaussianize

n number of nonmissing observations

norm\_stat Pearson's P / degrees of freedom

standardize was the transformation standardized

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

log\_x

## References

Georg M. Goerg (2016). LambertW: An R package for Lambert W x F Random Variables. R package version 0.6.4.

Georg M. Goerg (2011): Lambert W random variables - a new family of generalized skewed distributions with applications to risk estimation. Annals of Applied Statistics 3(5). 2197-2230.

Georg M. Goerg (2014): The Lambert Way to Gaussianize heavy-tailed data with the inverse of Tukey's h transformation as a special case. The Scientific World Journal.

## See Also

Gaussianize

## **Examples**

```
## Not run:
x <- rgamma(100, 1, 1)

lambert_obj <- lambert(x)
lambert_obj
p <- predict(lambert_obj)
x2 <- predict(lambert_obj, newdata = p, inverse = TRUE)

all.equal(x2, x)
## End(Not run)</pre>
```

log\_x

Log(x + a) Transformation

## **Description**

Perform a log\_b (x+a) normalization transformation

#### **Usage**

```
log_x(x, a = NULL, b = 10, standardize = TRUE, eps = 0.001, warn = TRUE, ...)
## S3 method for class 'log_x'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'log_x'
print(x, ...)
```

 $\log_x$ 

## **Arguments**

x A vector to normalize with with x

a The constant to add to x (defaults to max(0, -min(x) + eps)); see bestLogConstant

b The base of the log (defaults to 10)

standardize If TRUE, the transformed values are also centered and scaled, such that the

transformation attempts a standard normal

eps The allowed error in the expression for the selected a

warn Should a warning result from infinite values?

... additional arguments
object an object of class 'log\_x'

newdata a vector of data to be (potentially reverse) transformed

inverse if TRUE, performs reverse transformation

## **Details**

log\_x performs a simple log transformation in the context of bestNormalize, such that it creates a transformation that can be estimated and applied to new data via the predict function. The parameter a is essentially estimated by the training set by default (estimated as the minimum possible to some extent epsilon), while the base must be specified beforehand.

#### Value

A list of class log\_x with elements

x.t transformed original data

x original data

mean after transformation but prior to standardization sd sd after transformation but prior to standardization

a estimated a valueb estimated base b value

n number of nonmissing observations norm\_stat Pearson's P / degrees of freedom standardize was the transformation standardized

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

## **Examples**

```
x <- rgamma(100, 1, 1)

log_x_obj <- log_x(x)
log_x_obj
p <- predict(log_x_obj)
x2 <- predict(log_x_obj, newdata = p, inverse = TRUE)</pre>
```

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```
all.equal(x2, x)
```

no\_transform

Identity transformation and center/scale transform

## **Description**

Perform an identity transformation. Admittedly it seems odd to have a dedicated function to essentially do I(x), but it makes sense to keep the same syntax as the other transformations so it plays nicely with them. As a benefit, the bestNormalize function will also show a comparable normalization statistic for the untransformed data. If standardize == TRUE, center\_scale passes to bestNormalize instead.

## Usage

```
no_transform(x, warn = TRUE, ...)
## S3 method for class 'no_transform'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'no_transform'
print(x, ...)

center_scale(x, warn = TRUE, ...)
## S3 method for class 'center_scale'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'center_scale'
print(x, ...)
## S3 method for class 'no_transform'
tidy(x, ...)
```

## Arguments

X	A 'no_transform' object.
warn	Should a warning result from infinite values?
	not used
object	an object of class 'no_transform'
newdata	a vector of data to be (potentially reverse) transformed
inverse	if TRUE, performs reverse transformation

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#### **Details**

no\_transform creates a identity transformation object that can be applied to new data via the predict function.

#### Value

A list of class no\_transform with elements

x.t transformed original data

x original data

n number of nonmissing observations

norm\_stat Pearson's P / degrees of freedom

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

#### **Examples**

```
x <- rgamma(100, 1, 1)
no_transform_obj <- no_transform(x)
no_transform_obj
p <- predict(no_transform_obj)
x2 <- predict(no_transform_obj, newdata = p, inverse = TRUE)
all.equal(x2, x)</pre>
```

orderNorm

Calculate and perform Ordered Quantile normalizing transformation

## **Description**

The Ordered Quantile (ORQ) normalization transformation, orderNorm(), is a rank-based procedure by which the values of a vector are mapped to their percentile, which is then mapped to the same percentile of the normal distribution. Without the presence of ties, this essentially guarantees that the transformation leads to a uniform distribution.

The transformation is:

$$g(x) = \Phi^{-1}((rank(x) - .5)/(length(x)))$$

Where  $\Phi$  refers to the standard normal cdf, rank(x) refers to each observation's rank, and length(x) refers to the number of observations.

By itself, this method is certainly not new; the earliest mention of it that I could find is in a 1947 paper by Bartlett (see references). This formula was outlined explicitly in Van der Waerden, and expounded upon in Beasley (2009). However there is a key difference to this version of it, as explained below.

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Using linear interpolation between these percentiles, the ORQ normalization becomes a 1-1 transformation that can be applied to new data. However, outside of the observed domain of x, it is unclear how to extrapolate the transformation. In the ORQ normalization procedure, a binomial glm with a logit link is used on the ranks in order to extrapolate beyond the bounds of the original domain of x. The inverse normal CDF is then applied to these extrapolated predictions in order to extrapolate the transformation. This mitigates the influence of heavy-tailed distributions while preserving the 1-1 nature of the transformation. The extrapolation will provide a warning unless warn = FALSE.) However, we found that the extrapolation was able to perform very well even on data as heavy-tailed as a Cauchy distribution (paper to be published).

The fit used to perform the extrapolation uses a default of 10000 observations (or length(x) if that is less). This added approximation improves the scalability, both computationally and in terms of memory used. Do not set this value to be too low (e.g. <100), as there is no benefit to doing so. Increase if your test data set is large relative to 10000 and/or if you are worried about losing signal in the extremes of the range.

This transformation can be performed on new data and inverted via the predict function.

## Usage

```
orderNorm(x, n_logit_fit = min(length(x), 10000), ..., warn = TRUE)
## S3 method for class 'orderNorm'
predict(object, newdata = NULL, inverse = FALSE, warn = TRUE, ...)
## S3 method for class 'orderNorm'
print(x, ...)
```

## **Arguments**

x A vector to normalize

n\_logit\_fit Number of points used to fit logit approximation

... additional arguments

warn transforms outside observed range or ties will yield warning

object an object of class 'orderNorm'

newdata a vector of data to be (reverse) transformed inverse if TRUE, performs reverse transformation

#### Value

A list of class orderNorm with elements

x.t transformed original data

x original data

n number of nonmissing observations

ties\_status indicator if ties are present

fit fit to be used for extrapolation, if needed

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```
norm_stat Pearson's P / degrees of freedom
```

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

## References

Bartlett, M. S. "The Use of Transformations." Biometrics, vol. 3, no. 1, 1947, pp. 39-52. JSTOR www.jstor.org/stable/3001536.

Van der Waerden BL. Order tests for the two-sample problem and their power. 1952;55:453-458. Ser A.

Beasley TM, Erickson S, Allison DB. Rank-based inverse normal transformations are increasingly used, but are they merited? Behav. Genet. 2009;39(5): 580-595. pmid:19526352

#### See Also

```
boxcox, lambert, bestNormalize, yeojohnson
```

## **Examples**

```
x <- rgamma(100, 1, 1)

orderNorm_obj <- orderNorm(x)

orderNorm_obj
p <- predict(orderNorm_obj)
x2 <- predict(orderNorm_obj, newdata = p, inverse = TRUE)

all.equal(x2, x)</pre>
```

plot.bestNormalize

Transformation plotting

## Description

Plots transformation functions for objects produced by the bestNormalize package

## Usage

```
## S3 method for class 'bestNormalize'
plot(
    x,
    inverse = FALSE,
    bounds = NULL,
    cols = NULL,
    methods = NULL,
    leg_loc = "top",
    ...
)
```

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```
## S3 method for class 'orderNorm'
plot(x, inverse = FALSE, bounds = NULL, ...)
## S3 method for class 'boxcox'
plot(x, inverse = FALSE, bounds = NULL, ...)
## S3 method for class 'yeojohnson'
plot(x, inverse = FALSE, bounds = NULL, ...)
## S3 method for class 'lambert'
plot(x, inverse = FALSE, bounds = NULL, ...)
```

## Arguments

X	a fitted transformation
inverse	if TRUE, plots the inverse transformation
bounds	a vector of bounds to plot for the transformation
cols	a vector of colors to use for the transforms (see details)
methods	a vector of transformations to plot
leg_loc	the location of the legend on the plot
	further parameters to be passed to plot and lines

## **Details**

The plots produced by the individual transformations are simply plots of the original values by the newly transformed values, with a line denoting where transformations would take place for new data.

For the bestNormalize object, this plots each of the possible transformations run by the original call to bestNormalize. The first argument in the "cols" parameter refers to the color of the chosen transformation.

sqrt\_x

sqrt(x + a) Normalization

## **Description**

Perform a sqrt (x+a) normalization transformation

## Usage

```
sqrt_x(x, a = NULL, standardize = TRUE, ...)
## S3 method for class 'sqrt_x'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'sqrt_x'
print(x, ...)
```

24 sqrt\_x

## **Arguments**

x A vector to normalize with with x

The constant to add to x (defaults to max(0, -min(x)))

standardize If TRUE, the transformed values are also centered and scaled, such that the

transformation attempts a standard normal

... additional arguments object an object of class 'sqrt\_x'

newdata a vector of data to be (potentially reverse) transformed

inverse if TRUE, performs reverse transformation

## **Details**

sqrt\_x performs a simple square-root transformation in the context of bestNormalize, such that it creates a transformation that can be estimated and applied to new data via the predict function. The parameter a is essentially estimated by the training set by default (estimated as the minimum possible), while the base must be specified beforehand.

#### Value

A list of class sqrt\_x with elements

x.t transformed original data

x original data

mean after transformation but prior to standardization sd after transformation but prior to standardization

n number of nonmissing observations norm\_stat Pearson's P / degrees of freedom standardize was the transformation standardized

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

## Examples

```
x <- rgamma(100, 1, 1)
sqrt_x_obj <- sqrt_x(x)
sqrt_x_obj
p <- predict(sqrt_x_obj)
x2 <- predict(sqrt_x_obj, newdata = p, inverse = TRUE)
all.equal(x2, x)</pre>
```

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step\_best\_normalize

Run bestNormalize transformation for recipes implementation

## **Description**

'step\_best\_normalize' creates a specification of a recipe step (see 'recipes' package) that will transform data using the best of a suite of normalization transformations estimated (by default) using cross-validation.

## Usage

```
step_best_normalize(
  recipe,
  ...,
  role = NA,
  trained = FALSE,
  transform_info = NULL,
  transform_options = list(),
  num_unique = 5,
  skip = FALSE,
  id = rand_id("best_normalize")
)

## S3 method for class 'step_best_normalize'
tidy(x, ...)

## S3 method for class 'step_best_normalize'
axe_env(x, ...)
```

## Arguments

•	A C 1	
racina	A tormula or	recine
recipe	A formula or	rccipc

... One or more selector functions to choose which variables are affected by the

step. See [selections()] for more details. For the 'tidy' method, these are not

currently used.

role Not used by this step since no new variables are created.

trained For recipes functionality

transform\_info A numeric vector of transformation values. This (was transform\_info) is 'NULL'

until computed by [prep.recipe()].

 ${\tt transform\_options}$ 

options to be passed to bestNormalize

num\_unique An integer where data that have less possible values will not be evaluate for a

transformation.

skip For recipes functionality id For recipes functionality

x A 'step\_best\_normalize' object.

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#### **Details**

The bestnormalize transformation can be used to rescale a variable to be more similar to a normal distribution. See '?bestNormalize' for more information; 'step\_best\_normalize' is the implementation of 'bestNormalize' in the 'recipes' context.

As of version 1.7, the 'butcher' package can be used to (hopefully) improve scalability of this function on bigger data sets.

#### Value

An updated version of 'recipe' with the new step added to the sequence of existing steps (if any). For the 'tidy' method, a tibble with columns 'terms' (the selectors or variables selected) and 'value' (the lambda estimate).

#### See Also

bestNormalize orderNorm, [recipe()] [prep.recipe()] [bake.recipe()]

## **Examples**

```
library(recipes)
rec <- recipe(~ ., data = as.data.frame(iris))

bn_trans <- step_best_normalize(rec, all_numeric())

bn_estimates <- prep(bn_trans, training = as.data.frame(iris))

bn_data <- bake(bn_estimates, as.data.frame(iris))

plot(density(iris[, "Petal.Length"]), main = "before")
plot(density(bn_data$Petal.Length), main = "after")

tidy(bn_trans, number = 1)
tidy(bn_estimates, number = 1)</pre>
```

step\_orderNorm

ORQ normalization (orderNorm) for recipes implementation

## **Description**

'step\_orderNorm' creates a specification of a recipe step (see 'recipes' package) that will transform data using the ORQ (orderNorm) transformation, which approximates the "true" normalizing transformation if one exists. This is considerably faster than 'step\_bestNormalize'.

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## Usage

```
step_orderNorm(
  recipe,
    ...,
  role = NA,
  trained = FALSE,
  transform_info = NULL,
  transform_options = list(),
  num_unique = 5,
  skip = FALSE,
  id = rand_id("orderNorm")
)

## S3 method for class 'step_orderNorm'
tidy(x, ...)

## S3 method for class 'step_orderNorm'
axe_env(x, ...)
```

## **Arguments**

recipe	A formula c	

... One or more selector functions to choose which variables are affected by the

step. See [selections()] for more details. For the 'tidy' method, these are not

currently used.

role Not used by this step since no new variables are created.

trained For recipes functionality

transform\_info A numeric vector of transformation values. This (was transform\_info) is 'NULL'

until computed by [prep.recipe()].

transform\_options

options to be passed to orderNorm

num\_unique An integer where data that have less possible values will not be evaluate for a

transformation.

skip For recipes functionality

id For recipes functionality

x A 'step\_orderNorm' object.

#### **Details**

The orderNorm transformation can be used to rescale a variable to be more similar to a normal distribution. See '?orderNorm' for more information; 'step\_orderNorm' is the implementation of 'orderNorm' in the 'recipes' context.

As of version 1.7, the 'butcher' package can be used to (hopefully) improve scalability of this function on bigger data sets.

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## Value

An updated version of 'recipe' with the new step added to the sequence of existing steps (if any). For the 'tidy' method, a tibble with columns 'terms' (the selectors or variables selected) and 'value' (the lambda estimate).

#### References

Ryan A. Peterson (2019). Ordered quantile normalization: a semiparametric transformation built for the cross-validation era. Journal of Applied Statistics, 1-16.

## See Also

```
orderNorm bestNormalize, [recipe()] [prep.recipe()] [bake.recipe()]
```

## **Examples**

```
library(recipes)
rec <- recipe(~ ., data = as.data.frame(iris))

orq_trans <- step_orderNorm(rec, all_numeric())

orq_estimates <- prep(orq_trans, training = as.data.frame(iris))

orq_data <- bake(orq_estimates, as.data.frame(iris))

plot(density(iris[, "Petal.Length"]), main = "before")
plot(density(orq_data$Petal.Length), main = "after")

tidy(orq_trans, number = 1)
tidy(orq_estimates, number = 1)</pre>
```

yeojohnson

Yeo-Johnson Normalization

## **Description**

Perform a Yeo-Johnson Transformation and center/scale a vector to attempt normalization

## Usage

```
yeojohnson(x, eps = 0.001, standardize = TRUE, ...)
## S3 method for class 'yeojohnson'
predict(object, newdata = NULL, inverse = FALSE, ...)
## S3 method for class 'yeojohnson'
print(x, ...)
```

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#### **Arguments**

x A vector to normalize with Yeo-Johnson

eps A value to compare lambda against to see if it is equal to zero

transformation attempts a standard normal

.. Additional arguments that can be passed to the estimation of the lambda param-

eter (lower, upper)

object an object of class 'yeojohnson'

newdata a vector of data to be (reverse) transformed inverse if TRUE, performs reverse transformation

## **Details**

yeojohnson estimates the optimal value of lambda for the Yeo-Johnson transformation. This transformation can be performed on new data, and inverted, via the predict function.

The Yeo-Johnson is similar to the Box-Cox method, however it allows for the transformation of nonpositive data as well. The step\_YeoJohnson function in the recipes package is another useful resource (see references).

#### Value

A list of class yeojohnson with elements

x.t transformed original data

x original data

mean mean after transformation but prior to standardization
sd sd after transformation but prior to standardization
lambda estimated lambda value for skew transformation

n number of nonmissing observations
norm\_stat Pearson's P / degrees of freedom
standardize Was the transformation standardized

The predict function returns the numeric value of the transformation performed on new data, and allows for the inverse transformation as well.

#### References

Yeo, I. K., & Johnson, R. A. (2000). A new family of power transformations to improve normality or symmetry. Biometrika.

Max Kuhn and Hadley Wickham (2017). recipes: Preprocessing Tools to Create Design Matrices. R package version 0.1.0.9000. https://github.com/topepo/recipes

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## **Examples**

```
x <- rgamma(100, 1, 1)
yeojohnson_obj <- yeojohnson(x)
yeojohnson_obj
p <- predict(yeojohnson_obj)
x2 <- predict(yeojohnson_obj, newdata = p, inverse = TRUE)
all.equal(x2, x)</pre>
```

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