

Package ‘nlraa’

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Version 1.9.10

Title Nonlinear Regression for Agricultural Applications

Description Additional nonlinear regression functions using self-start (SS) algorithms. One of the functions is the Beta growth function proposed by Yin et al. (2003) <[doi:10.1093/aob/mcg029](https://doi.org/10.1093/aob/mcg029)>. There are several other functions with breakpoints (e.g. linear-plateau, plateau-linear, exponential-plateau, plateau-exponential, quadratic-plateau, plateau-quadratic and bilinear), a non-rectangular hyperbola and a bell-shaped curve. Twenty eight (28) new self-start (SS) functions in total. This package also supports the publication 'Nonlinear regression Models and applications in agricultural research' by Archontoulis and Miguez (2015) <[doi:10.2134/agronj2012.0506](https://doi.org/10.2134/agronj2012.0506)>, a book chapter with similar material <[doi:10.2134/appliedstatistics.2016.0003.c15](https://doi.org/10.2134/appliedstatistics.2016.0003.c15)> and a publication by Oddi et. al. (2019) in Ecology and Evolution <[doi:10.1002/ece3.5543](https://doi.org/10.1002/ece3.5543)>. The function 'nlsLMList' uses 'nlsLM' for fitting, but it is otherwise almost identical to 'nlme::nlsList'. In addition, this release of the package provides functions for conducting simulations for 'nlme' and 'gnls' objects as well as bootstrapping. These functions are intended to work with the modeling framework of the 'nlme' package. It also provides four vignettes with extended examples.

Depends R (>= 3.5.0)

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Encoding UTF-8

VignetteBuilder knitr

BugReports <https://github.com/femiguez/nlraa/issues>

Imports boot, knitr, MASS, Matrix, mgcv, nlme, stats

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barley*Barley response to nitrogen fertilizer***Description**

Data from a paper by Arild Vold on response of barley to nitrogen fertilizer

Usage

```
barley
```

Format

A data frame with 76 rows and 3 columns

year Year when the trial was conducted (1970-1988).

NF Nitrogen fertilizer (g/m²).

yield Grain yield of barley (g/m²).

Source

Aril Vold (1998). A generalization of ordinary yield response functions. Ecological Applications. 108:227-236.

boot_lm*Bootstrapping for linear models***Description**

Bootstrapping for linear models

Usage

```
boot_lm(
  object,
  f = NULL,
  R = 999,
  psim = 2,
  resid.type = c("resample", "normal", "wild"),
  data = NULL,
  verbose = TRUE,
  ...
)
```

Arguments

object	object of class <code>lm</code>
f	function to be applied (and bootstrapped), default <code>coef</code>
R	number of bootstrap samples, default 999
psim	simulation level for <code>simulate_lm</code>
resid.type	either “resample”, “normal” or “wild”.
data	optional data argument (useful/needed when data are not in an available environment).
verbose	logical (default TRUE) whether to print message if model does not converge. (rare for linear models).
...	additional arguments to be passed to function <code>boot</code>

Details

The residuals can either be generated by resampling with replacement (default), from a normal distribution (parameteric) or by changing their signs (wild). This last one is called “wild bootstrap”.

Note

at the moment, when the argument `data` is used, it is not possible to check that it matches the original data used to fit the model. It will also override the fetching of data.

Examples

```
require(car)
data(barley, package = "nlraa")
## Fit a linear model (quadratic)
fit.lm <- lm(yield ~ NF + I(NF^2), data = barley)

## Bootstrap coefficients by default
fit.lm.bt <- boot_lm(fit.lm)
## Compute confidence intervals
confint(fit.lm.bt, type = "perc")
## Visualize
hist(fit.lm.bt, 1, ci = "perc", main = "Intercept")
hist(fit.lm.bt, 2, ci = "perc", main = "NF term")
hist(fit.lm.bt, 3, ci = "perc", main = "I(NF^2) term")
```

`boot_lme`*Bootstrapping for linear mixed models*

Description

Bootstrapping tools for linear mixed-models using a consistent interface
 bootstrap function for objects of class [gls](#)

Usage

```
boot_lme(
  object,
  f = NULL,
  R = 999,
  psim = 1,
  cores = 1L,
  data = NULL,
  verbose = TRUE,
  ...
)

boot_gls(
  object,
  f = NULL,
  R = 999,
  psim = 1,
  cores = 1L,
  data = NULL,
  verbose = TRUE,
  ...
)
```

Arguments

<code>object</code>	object of class lme or gls
<code>f</code>	function to be applied (and bootstrapped), default <code>coef(gls)</code> or <code>fixef(lme)</code>
<code>R</code>	number of bootstrap samples, default 999
<code>psim</code>	simulation level for vector of fixed parameters either for simulate_gls or simulate_lme
<code>cores</code>	number of cores to use for parallel computation
<code>data</code>	optional data argument (useful/needed when data are not in an available environment).
<code>verbose</code>	logical (default TRUE) whether to print a message if model does not converge.
<code>...</code>	additional arguments to be passed to function <code>boot</code>

Details

This function is inspired by [Boot](#), which does not seem to work with ‘gls’ or ‘lme’ objects. This function makes multiple copies of the original data, so it can be very hungry in terms of memory use, but I do not believe this to be a big problem given the models we typically fit.

Examples

```
require(nlme)
require(car)
data(Orange)

fm1 <- lme(circumference ~ age, random = ~ 1 | Tree, data = Orange)
fm1.bt <- boot_lme(fm1, R = 50)

hist(fm1.bt)
```

boot_nlme

Bootstrapping for generalized nonlinear models and nonlinear mixed models

Description

Bootstrapping tools for nonlinear models using a consistent interface
bootstrap function for objects of class [gnls](#)

Usage

```
boot_nlme(
  object,
  f = NULL,
  R = 999,
  psim = 1,
  cores = 1L,
  data = NULL,
  verbose = TRUE,
  ...
)

boot_gnls(
  object,
  f = NULL,
  R = 999,
  psim = 1,
  cores = 1L,
```

```
  data = NULL,
  verbose = TRUE,
  ...
)
```

Arguments

object	object of class <code>nlme</code> or <code>gnls</code>
f	function to be applied (and bootstrapped), default <code>coef</code> (<code>gnls</code>) or <code>fixef</code> (<code>nlme</code>)
R	number of bootstrap samples, default 999
psim	simulation level for vector of fixed parameters either for <code>simulate_gnls</code> or <code>simulate_nlme_one</code>
cores	number of cores to use for parallel computation
data	optional data argument (useful/needed when data are not in an available environment).
verbose	logical (default TRUE) whether to print a message if model does not converge.
...	additional arguments to be passed to function <code>boot</code>

Details

This function is inspired by `Boot`, which does not seem to work with '`gnls`' or '`nlme`' objects. This function makes multiple copies of the original data, so it can be very hungry in terms of memory use, but I do not believe this to be a big problem given the models we typically fit.

Examples

```
require(car)
require(nlme)
data(barley, package = "nlraa")
barley2 <- subset(barley, year < 1974)
fit.lp.gnls2 <- gnls(yield ~ SSlinp(NF, a, b, xs), data = barley2)
barley2$year.f <- as.factor(barley2$year)
cfs <- coef(fit.lp.gnls2)
fit.lp.gnls3 <- update(fit.lp.gnls2,
                        params = list(a + b + xs ~ year.f),
                        start = c(cfs[1], 0, 0, 0,
                                  cfs[2], 0, 0, 0,
                                  cfs[3], 0, 0, 0))
## This will take a few seconds
fit.lp.gnls.Bt3 <- boot_nlme(fit.lp.gnls3, R = 300)
confint(fit.lp.gnls.Bt3, type = "perc")
```

boot_nls*Bootstrapping for nonlinear models*

Description

Bootstrapping for nonlinear models

Usage

```
boot_nls(  
  object,  
  f = NULL,  
  R = 999,  
  psim = 2,  
  resid.type = c("resample", "normal", "wild"),  
  data = NULL,  
  verbose = TRUE,  
  ...  
)
```

Arguments

object	object of class nls
f	function to be applied (and bootstrapped), default coef
R	number of bootstrap samples, default 999
psim	simulation level for simulate_nls
resid.type	either “resample”, “normal” or “wild”.
data	optional data argument (useful/needed when data are not in an available environment).
verbose	logical (default TRUE) whether to print a message if model does not converge.
...	additional arguments to be passed to function boot

Details

The residuals can either be generated by resampling with replacement (default or non-parametric), from a normal distribution (parameteric) or by changing their signs (wild). This last one is called “wild bootstrap”. There is more information in [boot_lm](#).

Note

at the moment, when the argument data is used, it is not possible to check that it matches the original data used to fit the model. It will also override the fetching of data.

See Also

[Boot](#)

Examples

```
require(car)
data(barley, package = "nlraa")
## Fit a linear-plateau
fit.nls <- nls(yield ~ SSlinp(NF, a, b, xs), data = barley)

## Bootstrap coefficients by default
## Keeping R small for simplicity, increase R for a more realistic use
fit.nls.bt <- boot_nls(fit.nls, R = 1e2)
## Compute confidence intervals
confint(fit.nls.bt, type = "perc")
## Visualize
hist(fit.nls.bt, 1, ci = "perc", main = "Intercept")
hist(fit.nls.bt, 2, ci = "perc", main = "linear term")
hist(fit.nls.bt, 3, ci = "perc", main = "xs break-point term")
```

`confidence_intervals` *Confidence interval methods for (non)-linear models*

Description

Confidence interval methods for (non)-linear models. Method ‘wald’ for objects of class ‘nls’ uses `confint.default`

Usage

```
confidence_intervals(
  x,
  method = c("wald", "profile", "bootstrap", "simple-bayes", "all"),
  parm,
  level = 0.95,
  verbose = FALSE,
  ...
)
```

Arguments

<code>x</code>	object of class <code>lm</code> , <code>nls</code> , <code>nlme</code> , <code>gls</code> or <code>gnls</code>
<code>method</code>	method or methods to use. Possible options are: ‘wald’, ‘profile’, ‘bootstrap’, ‘all’
<code>parm</code>	optional character string to select the parameter
<code>level</code>	probability level
<code>verbose</code>	logical (default FALSE) whether to print messages
<code>...</code>	additional arguments to be passed to function <code>boot</code>

Examples

```
require(car)
data(barley, package = "nlraa")
## Fit a linear model (quadratic)
fit.lm <- lm(yield ~ NF + I(NF^2), data = barley)

cfs.int <- confidence_intervals(fit.lm, method = c("wald", "bootstrap"))

fit.nls <- nls(yield ~ SSlinp(NF, a, b, xs), data = barley)

cfs.int2 <- confidence_intervals(fit.nls, method = c("wald", "profile", "bootstrap"))
```

fm1.P.at.x.0.4*object for confidence bands vignette fm1.P.at.x.0.4***Description**

object for confidence bands vignette fm1.P.at.x.0.4

Usage**fm1.P.at.x.0.4****Format**

An object of class ‘boot’

fm1.P.at.x.0.4 object created in the vignette in chunk ‘Puromycin-6’**Source**

this package vignette

fm1.P.bt*object for confidence bands vignette fm1.P.bt***Description**

object for confidence bands vignette fm1.P.bt

Usage**fm1.P.bt**

Format

An object of class ‘boot’

fm1.P.bt object created in the vignette in chunk ‘Puromycin-2’

Source

this package vignette

fm1.P.bt.ft

object for confidence bands vignette fm1.P.bt.ft

Description

object for confidence bands vignette fm1.P.bt.ft

Usage

fm1.P.bt.ft

Format

An object of class ‘boot’

fm1.P.bt.ft object created in the vignette in chunk ‘Puromycin-4’

Source

this package vignette

fm2.Lob.bt

object for confidence bands vignette fm2.Lob.bt

Description

object for confidence bands vignette fm2.Lob.bt

Usage

fm2.Lob.bt

Format

An object of class ‘boot’

fm2.Lob.bt object created in the vignette in chunk ‘Loblolly-methods-2’

Source

this package vignette

fmm1.bt*object for confidence bands vignette fmm1.bt*

Description

object for confidence bands vignette fmm1.bt

Usage

```
fmm1.bt
```

Format

An object of class ‘boot’

fmm1.bt object created in the vignette in chunk ‘maizeleafext-2’

Source

this package vignette

IA_tab*Indexes of Agreement Table*

Description

Indexes of agreement

printing function for IA_tab

plotting function for a IA_tab, it requires ‘ggplot2’

Usage

```
IA_tab(obs, sim, object, null.object)

## S3 method for class 'IA_tab'
print(x, ..., digits = 2)

## S3 method for class 'IA_tab'
plot(x, y, ..., type = c("OvsS", "RvsS"))
```

Arguments

<code>obs</code>	vector with observed data
<code>sim</code>	vector with simulated data (should be the same length as observed)
<code>object</code>	alternative to the previous two arguments. An object of class ‘lm’, ‘nls’, ‘lme’ or ‘nlme’
<code>null.object</code>	optional object which represents the ‘null’ model. It is an intercept-only model by default. (Not used at the moment).
<code>x</code>	object of class ‘IA_tab’.
<code>...</code>	additional plotting arguments (none use at the moment).
<code>digits</code>	number of digits for rounding (default is 2)
<code>y</code>	not used at the moment
<code>type</code>	either “OvsS” (observed vs. simulated) or “RvsS” (residuals vs. simulated).

Details

This function returns several indexes that might be useful for interpretation. Notice that bias (mean), rss, mse and rmse are model-free

The intercept, slope, reg.rss, reg.mse and reg.rmse are based on a regression model

For objects of class ‘lm’ and ‘nls’

bias: `mean(obs - sim)`

intercept: intercept of the model `obs ~ beta_0 + beta_1 * sim + error`

slope: slope of the model `obs ~ beta_0 + beta_1 * sim + error`

rss: residual sum of squares (model free)

mse: mean squared error (model free)

rmse: root mean squared error (model free)

reg. rss (deviance): residual sum of squares of the previous model

reg. mse (reg. rss / n): mean squared error; where n is the number of observations

reg. rmse: squared root of the previous index

R2.1: R-squared extracted from an ‘lm’ object

R2.2: R-squared computed as the correlation between observed and simulated to the power of 2.

ME: model efficiency

NME: Normalized model efficiency

Corr: correlation between observed and simulated

ConCorr: concordance correlation

For objects of class ‘lme’ or ‘nlme’ there is the marginal and conditional R2.

https://en.wikipedia.org/wiki/Coefficient_of_determination

https://en.wikipedia.org/wiki/Nash-Sutcliffe_model_efficiency_coefficient

https://en.wikipedia.org/wiki/Concordance_correlation_coefficient

See Also

[IC_tab](#)

Examples

```

require(nlme)
require(ggplot2)
## Fit a simple model and then compute IAs
data(swpg)
#' ## Linear model
fit0 <- lm(lfgr ~ ftsw + I(ftsw^2), data = swpg)
ias0 <- IA_tab(object = fit0)
ias0
## Nonlinear model
fit1 <- nls(lfgr ~ SSblin(ftsw, a, b, xs, c), data = swpg)
ias1 <- IA_tab(object = fit1)
ias1
plot(ias1)
## Linear Mixed Models
data(barley, package = "nlraa")
fit2 <- lme(yield ~ NF + I(NF^2), random = ~ 1 | year, data = barley)
ias2 <- IA_tab(object = fit2)
ias2
## Nonlinear Mixed Model
barleyG <- groupedData(yield ~ NF | year, data = barley)
fit3L <- nlsLMLList(yield ~ SSquadp3(NF, a, b, c), data = barleyG)
fit3 <- nlme(fit3L, random = pdDiag(a + b ~ 1))
ias3 <- IA_tab(object = fit3)
ias3
plot(ias3)
## Plotting model
prds <- predict_nlme(fit3, interval = "conf", plevel = 0)
barleyGA <- cbind(barleyG, prds)
ggplot(data = barleyGA, aes(x = NF, y = yield)) +
  geom_point() +
  geom_line(aes(y = Estimate)) +
  geom_ribbon(aes(ymin = Q2.5, ymax = Q97.5),
              fill = "purple", alpha = 0.2)
## R2M for model 2
R2M(fit2)
## R2M for model 3
R2M(fit3)

## Using IA_tab without a model
IA_tab(obs = swpg$lfgr, sim = fitted(fit0))

```

Description

Information criteria table with weights

Usage

```
IC_tab(..., criteria = c("AIC", "AICc", "BIC"), sort = TRUE)
```

Arguments

...	model fit objects fitted to the same data
criteria	either 'AIC', 'AICc' or 'BIC'.
sort	whether to sort by weights (default to TRUE)

Note

The delta and weights are calculated based on the 'criteria'

See Also

[ICtab](#)

lfmc

Live fuel moisture content

Description

Live fuel moisture content

Usage

lfmc

Format

A data frame with 247 rows and 5 variables:

leaf.type	-factor-	Species for which data was recorded ("Grass E", "Grass W", "M. spinosum", "S. bracteolactus")
time	-integer-	time in days 1-80
plot	-factor-	plot with levels 1-6 (discrete)
site	-factor-	either P ("East") or SR ("West")
lfmc	-numeric-	Live fuel moisture content (percent)
group		grouping for regression

Details

A dataset containing the leaf.type, time, plot, site and lfmc (live fuel mass concentration)

Source

[doi:10.1002/ece3.5543](https://doi.org/10.1002/ece3.5543)

Lob.bt.pe*object for confidence bands vignette Lob.bt.pe*

Description

object for confidence bands vignette Lob.bt.pe

Usage

`Lob.bt.pe`

Format

An object of class ‘boot’

Lob.bt.pe object created in the vignette in chunk ‘Loblolly-bootstrap-estimates-1’

Source

this package vignette

maizeleafext*Maize leaf extension rate as a response to temperature*

Description

Data on leaf extension rate as a response to meristem temperature in maize. The data are re-created liberally from Walls, W.R., 1971. Role of temperature in the regulation of leaf extension in *Zea mays*. *Nature*, 229: 46-47. The data points are not the same as in the original paper. Some additional points were inserted to fill in the blanks and allow for reasonable parameter estimates

Usage

`maizeleafext`

Format

A data frame with 10 rows and 2 columns

temp Meristem temperature (in Celsius).

rate Leaf extension rate (relative to 25 degrees).

Source

Walls, W.R., 1971. Role of temperature in the regulation of leaf extension in *Zea mays*. *Nature*, 229: 46-47.

nlraa.env

*Environment to store options and data for nlraa***Description**

Environment which stores indecies and data for bootstrapping mostly

Usage

```
nlraa.env
```

Format

An object of class `environment` of length 2.

Details

Create an nlraa environment for bootstrapping

nlsLMList

*Create a list of nls objects with the option of using nlsLM in addition to nls***Description**

This function is a copy of `[nlme::nlsList()]` from the ‘nlme’ package modified to use the `[minpack.lm::nlsLM()]` function in addition to (optionally) `[stats::nls()]`. By changing the algorithm argument it is possible to use `[stats::nls()]` as well

Usage

```
nlsLMList(
  model,
  data,
  start,
  control,
  level,
  subset,
  na.action = na.fail,
  algorithm = c("LM", "default", "port", "plinear"),
  lower = NULL,
  upper = NULL,
  pool = TRUE,
  warn.nls = NA
)
```

```

## S3 method for class 'selfStart'
nlsLMList(
  model,
  data,
  start,
  control,
  level,
  subset,
  na.action = na.fail,
  algorithm = c("LM", "default", "port", "plinear"),
  lower = NULL,
  upper = NULL,
  pool = TRUE,
  warn.nls = NA
)

```

Arguments

model	either a nonlinear model formula, with the response on the left of a ~ operator and an expression involving parameters, covariates, and a grouping factor separated by the operator on the right, or a selfStart function.
data	a data frame
start	list with starting values
control	control list, see [stats::nls()]
level	an optional integer specifying the level of grouping to be used when multiple nested levels of grouping are present.
subset	subset of rows to use
na.action	a function that indicates what should happen when the data contain NAs. The default action (na.fail) causes [nlme::nlsList()] to print an error message and terminate if there are any incomplete observations.
algorithm	choice of algorithm. Default is ‘LM’ which uses ‘nlsLM’ from the minpack.lm package. Other options are: “default”, “port” and “plinear” (nls).
lower	vectors of lower and upper bounds, replicated to be as long as start. If unspecified, all parameters are assumed to be unconstrained. Bounds can only be used with the “port” algorithm. They are ignored, with a warning, if given for other algorithms.
upper	see ‘lower’
pool	an optional logical value that is preserved as an attribute of the returned value. This will be used as the default for pool in calculations of standard deviations or standard errors for summaries.
warn.nls	logical indicating if nls errors (all of which are caught by tryCatch) should be signalled as a “summarizing” warning.

Details

See function [nlme::nlsList()] and [minpack.lm::nlsLM()]. This function is a copy of [nlme::nlsList()] but with minor changes to use LM instead as the default algorithm. The authors of the original function are Pinheiro and Bates.

Value

an object of class [nlme::nlsList()]
an object of class [nlsList](#)

Author(s)

Jose C. Pinheiro and Douglas M. Bates <bates@stat.wisc.edu> wrote the original [nlme::nlsList()]. Fernando E. Miguez made minor changes to use [minpack.lm::nlsLM()] in addition to (optionally) [stats::nls()]. R-Core maintains copyright after 2006.

nlsLMList.formula *Formula method for nls ‘LM’ list method*

Description

formula method for nlsLMList

Usage

```
## S3 method for class 'formula'
nlsLMList(
  model,
  data,
  start = NULL,
  control,
  level,
  subset,
  na.action = na.fail,
  algorithm = c("LM", "default", "port", "plinear"),
  lower = NULL,
  upper = NULL,
  pool = TRUE,
  warn.nls = NA
)
```

Arguments

model	see nlsList
data	see nlsList
start	see nlsList

control	see nls
level	see nlsList
subset	see nlsList
na.action	see nlsList
algorithm	choice of algorithm default is ‘LM’ which uses ‘nlsLM’ from the minpack.lm package.
lower	vectors of lower and upper bounds, replicated to be as long as start. If unspecified, all parameters are assumed to be unconstrained. Bounds can only be used with the “port” algorithm. They are ignored, with a warning, if given for other algorithms.
upper	see ‘lower’
pool	see nlsList
warn.nls	see nlsList

Value

an object of class [nlsList](#)

predict2_nls

*Prediction Bands for Nonlinear Regression***Description**

The method used in this function is described in Battes and Watts (2007) Nonlinear Regression Analysis and Its Applications (see pages 58-59). It is known as the Delta method.

Usage

```
predict2_nls(
  object,
  newdata = NULL,
  interval = c("none", "confidence", "prediction"),
  level = 0.95
)
```

Arguments

object	object of class ‘nls’
newdata	data frame with values for the predictor
interval	either ‘none’, ‘confidence’ or ‘prediction’
level	probability level (default is 0.95)

Details

This method is approximate and it works better when the distribution of the parameter estimates are normally distributed. This assumption can be evaluated by using bootstrap.

The method currently works well for any nonlinear function, but if predictions are needed on new data, then it is required that a selfStart function is used.

Value

a data frame with Estimate, Est.Error, lower interval bound and upper interval bound. For example, if the level = 0.95, the lower bound would be named Q2.5 and the upper bound would be name Q97.5

See Also

[predict.nls](#) and [predict_nls](#)

Examples

```
require(ggplot2)
require(nlme)
data(Soybean)

SoyF <- subset(Soybean, Variety == "F" & Year == 1988)
fm1 <- nls(weight ~ SSlogis(Time, Asym, xmid, scal), data = SoyF)
## The SSlogis also supplies analytical derivatives
## therefore the predict function returns the gradient too
prd1 <- predict(fm1, newdata = SoyF)

## Gradient
head(attr(prd1, "gradient"))
## Prediction method using gradient
prds <- predict2_nls(fm1, interval = "conf")
SoyFA <- cbind(SoyF, prds)
ggplot(data = SoyFA, aes(x = Time, y = weight)) +
  geom_point() +
  geom_line(aes(y = Estimate)) +
  geom_ribbon(aes(ymin = Q2.5, ymax = Q97.5), fill = "purple", alpha = 0.3) +
  ggtitle("95% Confidence Bands")

## This is equivalent
fm2 <- nls(weight ~ Asym/(1 + exp((xmid - Time)/scal)), data = SoyF,
            start = c(Asym = 20, xmid = 56, scal = 8))

## Prediction interval
prdi <- predict2_nls(fm1, interval = "pred")
SoyFA.PI <- cbind(SoyF, prdi)
## Make prediction interval plot
ggplot(data = SoyFA.PI, aes(x = Time, y = weight)) +
  geom_point() +
  geom_line(aes(y = Estimate)) +
  geom_ribbon(aes(ymin = Q2.5, ymax = Q97.5), fill = "purple", alpha = 0.3) +
```

```

ggttitle("95% Prediction Band")

## For these data we should be using gnls instead with an increasing variance
fm1 <- gnls(weight ~ SSlogis(Time, Asym, xmid, scal),
             data = SoyF, weights = varPower())

IC_tab(fm1, fm1)
prd <- predict_gnls(fm1, interval = "pred")
SoyFA.GPI <- cbind(SoyF, prd)

## These prediction bands are not perfect, but they could be smoothed
## to eliminate the ragged appearance
ggplot(data = SoyFA.GPI, aes(x = Time, y = weight)) +
  geom_point() +
  geom_line(aes(y = Estimate)) +
  geom_ribbon(aes(ymax = Q2.5, ymin = Q97.5), fill = "purple", alpha = 0.3) +
  ggttitle("95% Prediction Band. NLS model which \n accomodates an increasing variance")

```

predict_gam*Modified predicton function based on predict.gam***Description**

Largely based on predict.gam, but with some minor modifications to make it compatible with [predict_nls](#)

Usage

```

predict_gam(
  object,
  newdata = NULL,
  type = "link",
  se.fit = TRUE,
  terms = NULL,
  exclude = NULL,
  block.size = NULL,
  newdata.guaranteed = FALSE,
  na.action = na.pass,
  unconditional = FALSE,
  iterms.type = NULL,
  interval = c("none", "confidence", "prediction"),
  level = 0.95,
  tvalue = NULL,
  ...
)

```

Arguments

object	object of class ‘gam’ or as returned by function ‘gamm’
newdata	see predict.gam
type	see predict.gam
se.fit	see predict.gam . Notice that the default is changed to TRUE.
terms	see predict.gam
exclude	see predict.gam
block.size	see predict.gam
newdata.guaranteed	see predict.gam
na.action	see predict.gam
unconditional	see predict.gam
iterms.type	see predict.gam
interval	either ‘none’, ‘confidence’ or ‘prediction’.
level	probability level for the interval (default 0.95)
tvalue	t-value statistic used for constructing the intervals
...	additional arguments to be passed to predict.gam .

Value

numeric vector of the same length as the fitted object when interval is equal to ‘none’. Otherwise, a data.frame with columns named (for a 0.95 level) ‘Estimate’, ‘Est.Error’, ‘Q2.5’ and ‘Q97.5’

Note

this is a very simple wrapper for [predict.gam](#).

See Also

[predict.lm](#), [predict.nls](#), [predict.gam](#), [simulate_nls](#), [simulate_gam](#)

Examples

```
require(ggplot2)
require(mgcv)
data(barley)

fm.G <- gam(yield ~ s(NF, k = 6), data = barley)

## confidence and prediction intervals
cis <- predict_gam(fm.G, interval = "conf")
pis <- predict_gam(fm.G, interval = "pred")

barleyA.ci <- cbind(barley, cis)
barleyA.pi <- cbind(barley, pis)
```

```

ggplot() +
  geom_point(data = barleyA.ci, aes(x = NF, y = yield)) +
  geom_line(data = barleyA.ci, aes(x = NF, y = Estimate)) +
  geom_ribbon(data = barleyA.ci, aes(x = NF, ymin = Q2.5, ymax = Q97.5),
              color = "red", alpha = 0.3) +
  geom_ribbon(data = barleyA.pi, aes(x = NF, ymin = Q2.5, ymax = Q97.5),
              color = "blue", alpha = 0.3) +
  ggtitle("95% confidence and prediction bands")

```

predict_nlme

Average predictions from several (non)linear models based on IC weights

Description

Computes weights based on AIC, AICc, or BIC and it generates weighted predictions by the relative value of the IC values

`predict` function for objects of class [lme](#)

`predict` function for objects of class [gnls](#)

`predict` function for objects of class [gls](#)

Usage

```

predict_nlme(
  ...,
  criteria = c("AIC", "AICc", "BIC"),
  interval = c("none", "confidence", "prediction", "new-prediction"),
  level = 0.95,
  nsim = 1000,
  plevel = 0,
  newdata = NULL,
  weights
)

predict_lme(
  ...,
  criteria = c("AIC", "AICc", "BIC"),
  interval = c("none", "confidence", "prediction", "new-prediction"),
  level = 0.95,
  nsim = 1000,
  plevel = 0,
  newdata = NULL,
  weights
)

```

```

predict_gnls(
  ...,
  criteria = c("AIC", "AICc", "BIC"),
  interval = c("none", "confidence", "prediction", "new-prediction"),
  level = 0.95,
  nsim = 1000,
  plevel = 0,
  newdata = NULL,
  weights
)

predict_gls(
  ...,
  criteria = c("AIC", "AICc", "BIC"),
  interval = c("none", "confidence", "prediction", "new-prediction"),
  level = 0.95,
  nsim = 1000,
  plevel = 0,
  newdata = NULL,
  weights
)

```

Arguments

...	nlme, lme, gls or gnls objects.
criteria	either ‘AIC’, ‘AICc’ or ‘BIC’.
interval	either ‘none’, ‘confidence’ or ‘prediction’. It is also possible to choose ‘new-prediction’, which is a prediction that resamples the random effects (only relevant for ‘lme’ or ‘nlme’ objects.)
level	probability level for the interval (default 0.95)
nsim	number of simulations to perform for intervals. Default 1000.
plevel	parameter level prediction to be passed to prediction functions.
newdata	new data frame for predictions
weights	vector of weights of the same length as the number of models. It should sum up to one and it will override the information-criteria based weights. The weights should match the order of the models.

Value

numeric vector of the same length as the fitted object.

Note

all the objects should be fitted to the same data. The weights are based on the IC value.

See Also

[nlme::predict.nlme()] [nlme::predict.lme()] [nlme::predict.gnls()]

Examples

```

## Example
require(ggplot2)
require(nlme)
data(Orange)

## All models should be fitted using Maximum Likelihood
fm.L <- nlme(circumference ~ SSlogis(age, Asym, xmid, scal),
               random = pdDiag(Asym + xmid + scal ~ 1),
               method = "ML", data = Orange)
fm.G <- nlme(circumference ~ SSgompertz(age, Asym, b2, b3),
               random = pdDiag(Asym + b2 + b3 ~ 1),
               method = "ML", data = Orange)
fm.F <- nlme(circumference ~ SSfp1(age, A, B, xmid, scal),
               random = pdDiag(A + B + xmid + scal ~ 1),
               method = "ML", data = Orange)
fm.B <- nlme(circumference ~ SSbg4rp(age, w.max, lt.e, ldtm, ldtb),
               random = pdDiag(w.max + lt.e + ldtm + ldtb ~ 1),
               method = "ML", data = Orange)

## Print the table with weights
IC_tab(fm.L, fm.G, fm.F, fm.B)

## Each model prediction is weighted according to their AIC values
prd <- predict_nlme(fm.L, fm.G, fm.F, fm.B)

ggplot(data = Orange, aes(x = age, y = circumference)) +
  geom_point() +
  geom_line(aes(y = predict(fm.L, level = 0), color = "Logistic")) +
  geom_line(aes(y = predict(fm.G, level = 0), color = "Gompertz")) +
  geom_line(aes(y = predict(fm.F, level = 0), color = "4P-Logistic")) +
  geom_line(aes(y = predict(fm.B, level = 0), color = "Beta")) +
  geom_line(aes(y = prd, color = "Avg. Model"), linewidth = 1.2)

```

predict_nls

Average predictions from several (non)linear models based on IC weights

Description

Computes weights based on AIC, AICc, or BIC and it generates weighted predictions by the relative value of the IC values

predict function for objects of class [gam](#)

Usage

```

predict_nls(
  ...
)
```

```

criteria = c("AIC", "AICc", "BIC"),
interval = c("none", "confidence", "prediction"),
level = 0.95,
nsim = 1000,
resid.type = c("none", "resample", "normal", "wild"),
newdata = NULL,
weights
)
predict2_gam(
  ...,
  criteria = c("AIC", "AICc", "BIC"),
  interval = c("none", "confidence", "prediction"),
  level = 0.95,
  nsim = 1000,
  resid.type = c("none", "resample", "normal", "wild"),
  newdata = NULL,
  weights
)

```

Arguments

...	‘nls’ or ‘lm’ objects (‘glm’ and ‘gam’ objects inherit ‘lm’).
criteria	either ‘AIC’, ‘AICc’ or ‘BIC’.
interval	either ‘none’, ‘confidence’ or ‘prediction’.
level	probability level for the interval (default 0.95)
nsim	number of simulations to perform for intervals. Default 1000.
resid.type	either ‘none’, “resample”, “normal” or “wild”.
newdata	new data frame for predictions
weights	vector of weights of the same length as the number of models. It should sum up to one and it will override the information-criteria based weights. The weights should match the order of the models.

Value

numeric vector of the same length as the fitted object when interval is equal to ‘none’. Otherwise, a data.frame with columns named (for a 0.95 level) ‘Estimate’, ‘Est.Error’, ‘Q2.5’ and ‘Q97.5’

Note

all the objects should be fitted to the same data. Weights are based on the chosen IC value ($\exp(-0.5 * \text{delta IC})$). For models of class [mgcv::gam()] there is very limited support.

See Also

[stats::predict.lm()], [stats::predict.nls()], [mgcv::predict.gam()], [simulate_nls()], [simulate_gam()]

Examples

```
## Example
require(ggplot2)
require(mgcv)
data(barley, package = "nlraa")

fm.L <- lm(yield ~ NF, data = barley)
fm.Q <- lm(yield ~ NF + I(NF^2), data = barley)
fm.A <- nls(yield ~ SSasymp(NF, Asym, R0, lrc), data = barley)
fm(LP <- nls(yield ~ SSLinP(NF, a, b, xs), data = barley)
fm.QP <- nls(yield ~ SSquadP3(NF, a, b, c), data = barley)
fm.BL <- nls(yield ~ SSblin(NF, a, b, xs, c), data = barley)
fm.G <- gam(yield ~ s(NF, k = 6), data = barley)

## Print the table with weights
IC_tab(fm.L, fm.Q, fm.A, fm(LP, fm.QP, fm.BL, fm.G)

## Each model prediction is weighted according to their AIC values
prd <- predict_nls(fm.L, fm.Q, fm.A, fm(LP, fm.QP, fm.BL, fm.G)

ggplot(data = barley, aes(x = NF, y = yield)) +
  geom_point() +
  geom_line(aes(y = fitted(fm.L), color = "Linear")) +
  geom_line(aes(y = fitted(fm.Q), color = "Quadratic")) +
  geom_line(aes(y = fitted(fm.A), color = "Asymptotic")) +
  geom_line(aes(y = fitted(fm(LP), color = "Linear-plateau")) +
  geom_line(aes(y = fitted(fm.QP), color = "Quadratic-plateau")) +
  geom_line(aes(y = fitted(fm.BL), color = "Bi-linear")) +
  geom_line(aes(y = fitted(fm.G), color = "GAM")) +
  geom_line(aes(y = prd, color = "Avg. Model"), linewidth = 1.2)
```

print_boot

*Print an object of class **boot***

Description

This is a copy of `boot::print.boot`

Usage

```
print_boot(x, digits =getOption("digits"), index = 1L:ncol(boot.out$t), ...)
```

Arguments

- | | |
|---------------------|---|
| <code>x</code> | A bootstrap output object of class boot generated by one of the bootstrap functions. |
| <code>digits</code> | The number of digits to be printed in the summary statistics. |

- index Indices indicating for which elements of the bootstrap output summary statistics are required.
- ... further arguments passed to or from other methods.

Author(s)

Brian Ripley with a bug fix by John Nash

R2M

R-squared for nonlinear mixed models

Description

R-squared ‘modified’ for nonlinear (mixed) models

Usage

```
R2M(x, ...)

## S3 method for class 'nls'
R2M(x, ...)

## S3 method for class 'lm'
R2M(x, ...)

## S3 method for class 'gls'
R2M(x, ...)

## S3 method for class 'gnls'
R2M(x, ...)

## S3 method for class 'lme'
R2M(x, ...)

## S3 method for class 'nlme'
R2M(x, ...)
```

Arguments

- x object of class ‘lm’, ‘nls’, ‘gls’, ‘gnls’, ‘lme’ or ‘nlme’ .
- ... additional arguments (none use at the moment).

Details

I have read some papers about computing an R-squared for (non)linear (mixed) models and I am not sure that it makes sense at all. However, here they are and the method is general enough that it extends to nonlinear mixed models. What do these numbers mean and why would you want to compute them are good questions to ponder...

Recommended reading:

Nakagawa and Schielzeth Methods in Ecology and Evolution doi:[10.1111/j.2041210x.2012.00261.x](https://doi.org/10.1111/j.2041210x.2012.00261.x)

<https://stats.oarc.ucla.edu/other/mult-pkg/faq/general/faq-what-are-pseudo-r-squareds/>

Spiess, AN., Neumeyer, N. An evaluation of R² as an inadequate measure for nonlinear models in pharmacological and biochemical research: a Monte Carlo approach. BMC Pharmacol 10, 6 (2010). doi:[10.1186/14712210106](https://doi.org/10.1186/14712210106)

<https://stat.ethz.ch/pipermail/r-sig-mixed-models/2010q1/003363.html>

<https://blog.minitab.com/en/adventures-in-statistics-2/why-is-there-no-r-squared-for-nonlinear-reg>

[https://stats.stackexchange.com/questions/111150/calculating-r2-in-mixed-models-using-nakagawa-sch
225334#225334](https://stats.stackexchange.com/questions/111150/calculating-r2-in-mixed-models-using-nakagawa-sch)

Other R packages which calculate some version of an R-squared: performance, rcompanion, MuMin

Value

it returns a list with the following structure:
for an object of class ‘lm’, ‘nls’, ‘gls’ or ‘gnls’,
R2: R-squared
var.comp: variance components with var.fixed and var.resid
var.perc: variance components percents (should add up to 100)
for an object of class ‘lme’ or ‘nlme’ in addition it also returns:
R2.marginal: marginal R2 which only includes the fixed effects
R2.conditional: conditional R2 which includes both the fixed and random effects
var.random: the variance contribution of the random effects

Note

The references here strongly discourage the use of R-squared in anything but linear models.

See Also

[IA_tab](#)

Examples

```
require(nlme)
data(barley, package = "nlraa")
fit2 <- lme(yield ~ NF + I(NF^2), random = ~ 1 | year, data = barley)
R2M(fit2)
## Nonlinear Mixed Model
barleyG <- groupedData(yield ~ NF | year, data = barley)
fit3L <- nlsLMLList(yield ~ SSquadp3(NF, a, b, c), data = barleyG)
fit3 <- nlme(fit3L, random = pdDiag(a + b ~ 1))
R2M(fit3)
```

simulate_gam

Simulate responses from a generalized additive linear model gam

Description

By sampling from the vector of coefficients it is possible to simulate data from a ‘gam’ model.

Usage

```
simulate_gam(
  object,
  nsim = 1,
  psim = 1,
  resid.type = c("none", "resample", "normal", "wild"),
  value = c("matrix", "data.frame"),
  ...
)
```

Arguments

<code>object</code>	object of class <code>gam</code> or <code>glm</code> .
<code>nsim</code>	number of simulations to perform
<code>psim</code>	parameter simulation level (an integer, 0, 1, 2 or 3).
<code>resid.type</code>	type of residual to use. ‘none’, ‘resample’, ‘normal’ or ‘wild’.
<code>value</code>	either ‘matrix’ or ‘data.frame’
...	additional arguments (none used at the moment)

Details

This function is probably redundant. Simply using `simulate` generates data from the correct distribution for objects which inherit class `lm`. The difference is that I’m trying to add the uncertainty in the parameter estimates.

These are the options that control the parameter simulation level

psim = 0 returns the fitted values

psim = 1 simulates from a beta vector (mean response)

psim = 2 simulates observations according to the residual type (similar to observed data)

psim = 3 simulates a beta vector, considers uncertainty in the variance covariance matrix of beta and adds residuals (prediction)

The residual type (resid.type) controls how the residuals are generated. They are either resampled, simulated from a normal distribution or ‘wild’ where the Rademacher distribution is used (https://en.wikipedia.org/wiki/Rademacher_distribution). Resampled and normal both assume iid, but ‘normal’ makes the stronger assumption of normality. ‘wild’ does not assume constant variance, but it assumes symmetry.

Value

matrix or data.frame with responses

Note

psim = 3 is not implemented at the moment.

The purpose of this function is to make it compatible with other functions in this package. It has some limitations compared to the functions in the ‘see also’ section.

References

Generalized Additive Models. An Introduction with R. Second Edition. (2017) Simon N. Wood. CRC Press.

See Also

[predict](#), [predict.gam](#), [simulate](#) and [simulate_lm](#).

Examples

```
require(ggplot2)
require(mgcv)
## These count data are from GAM book by Simon Wood (pg. 132) - see reference
y <- c(12, 14, 33, 50, 67, 74, 123, 141, 165, 204, 253, 246, 240)
t <- 1:13
dat8 <- data.frame(y = y, t = t)
fit <- gam(y ~ t + I(t^2), family = poisson, data = dat8)
sims <- simulate_gam(fit, nsim = 100, value = "data.frame")

ggplot(data = sims) +
  geom_line(aes(x = t, y = sim.y, group = ii),
            color = "gray", alpha = 0.5) +
  geom_point(aes(x = t, y = y))
```

simulate_gls*Simulate fitted values from an object of class [gls](#)***Description**

Simulate values from an object of class gls. Unequal variances, as modeled using the ‘weights’ option are supported, and there is experimental code for dealing with the ‘correlation’ structure. This generates just one simulation from these type of models. To generate multiple simulations use [simulate_lme](#)

Usage

```
simulate_gls(
  object,
  psim = 1,
  na.action = na.fail,
  naPattern = NULL,
  data = NULL,
  ...
)
```

Arguments

<code>object</code>	object of class gls
<code>psim</code>	parameter simulation level, 0: for fitted values, 1: for simulation from fixed parameters (assuming a fixed vcov matrix), 2: for simulation considering the uncertainty in the residual standard error (sigma), this returns data which will appear similar to the observed values
<code>na.action</code>	default ‘na.fail’. See predict.gls
<code>naPattern</code>	missing value pattern. See predict.gls
<code>data</code>	the data argument is needed when using this function inside user defined functions. It should be identical to the data used to fit the model.
...	additional arguments (it is possible to supply a newdata this way)

Details

This function is based on [predict.gls](#) function

It uses function [mvrnorm](#) to generate new values for the coefficients of the model using the Variance-Covariance matrix [vcov](#). This variance-covariance matrix refers to the one for the parameters ‘beta’, not the one for the residuals.

Value

It returns a vector with simulated values with length equal to the number of rows in the original data

See Also

[predict.gls](#) [simulate_lme](#)

Examples

```
require(nlme)
data(Orange)

fit.gls <- gls(circumference ~ age, data = Orange,
                 weights = varPower())

## Visualize covariance matrix
fit.gls.vc <- var_cov(fit.gls)
image(log(fit.gls.vc[,ncol(fit.gls.vc):1]))

sim <- simulate_gnls(fit.gls)
```

simulate_gnls

Simulate fitted values from an object of class [gnls](#)

Description

Simulate values from an object of class `gnls`. Unequal variances, as modeled using the ‘weights’ option are supported, and there is experimental code for dealing with the ‘correlation’ structure.

Usage

```
simulate_gnls(
  object,
  psim = 1,
  na.action = na.fail,
  naPattern = NULL,
  data = NULL,
  ...
)
```

Arguments

<code>object</code>	object of class gnls
<code>psim</code>	parameter simulation level, 0: for fitted values, 1: for simulation from fixed parameters (assuming a fixed vcov matrix), 2: for simulation considering the uncertainty in the residual standard error (sigma), this returns data which will appear similar to the observed values
<code>na.action</code>	default ‘na.fail’. See predict.gnls
<code>naPattern</code>	missing value pattern. See predict.gnls

`data` the data argument is needed when using this function inside user defined functions. It should be identical to the data used to fit the model.
`...` additional arguments (it is possible to supply a newdata this way)

Details

This function is based on [predict.gnls](#) function

It uses function [mvrnorm](#) to generate new values for the coefficients of the model using the Variance-Covariance matrix [vcov](#). This variance-covariance matrix refers to the one for the parameters ‘beta’, not the one for the residuals.

Value

It returns a vector with simulated values with length equal to the number of rows in the original data

See Also

[predict.gnls](#)

Examples

```
require(nlme)
data(barley, package = "nlraa")

fit.gnls <- gnls(yield ~ SSlinp(NF, a, b, xs), data = barley)

sim <- simulate_gnls(fit.gnls)
```

simulate_lm

Simulate responses from a linear model lm

Description

The function [simulate](#) does not consider the uncertainty in the estimation of the model parameters. This function will attempt to do this.

Usage

```
simulate_lm(
  object,
  psim = 1,
  nsim = 1,
  resid.type = c("none", "resample", "normal", "wild"),
  value = c("matrix", "data.frame"),
  data = NULL,
  ...
)
```

Arguments

object	object of class <code>lm</code>
psim	parameter simulation level (an integer, 0, 1, 2, 3 or 4).
nsim	number of simulations to perform
resid.type	type of residual to include (none, resample, normal or wild)
value	either ‘matrix’ or ‘data.frame’
data	the data argument might be needed when using this function inside user defined functions. At least it is expected to be safer.
...	additional arguments (none used at the moment)

Details

Simulate responses from a linear model `lm`

These are the options that control the parameter simulation level

psim = 0 returns the fitted values

psim = 1 simulates a beta vector (mean response)

psim = 2 simulates a beta vector and adds resampled residuals (similar to observed data)

psim = 3 simulates a beta vector, considers uncertainty in the variance covariance matrix of beta and adds residuals (prediction)

psim = 4 only adds residuals according to resid.type (similar to `simulate.lm`)

The residual type (resid.type) controls how the residuals are generated. They are either resampled, simulated from a normal distribution or ‘wild’ where the Rademacher distribution is used (https://en.wikipedia.org/wiki/Rademacher_distribution). Resampled and normal both assume iid, but ‘normal’ makes the stronger assumption of normality. When psim = 2 and resid.type = none, `simulate` is used instead. ‘wild’ does not assume constant variance, but it assumes symmetry.

Value

matrix or data.frame with responses

References

See “Inference Based on the Wild Bootstrap” James G. MacKinnon <https://www.math.kth.se/matstat/gru/sf2930/papers/wild.bootstrap.pdf> “Bootstrap in Nonstationary Autoregression” Zuzana Praskova https://dml.cz/bitstream/handle/10338.dmlcz/135473/Kybernetika_38-2002-4-1.pdf “Jackknife, Bootstrap and other Resampling Methods in Regression Analysis” C. F. J. Wu. The Annals of Statistics. 1986. Vol 14. 1261-1295.

Examples

```
require(ggplot2)
data(Orange)
fit <- lm(circumference ~ age, data = Orange)
sims <- simulate_lm(fit, nsim = 100, value = "data.frame")
```

```
ggplot(data = sims) +
  geom_line(aes(x = age, y = sim.y, group = ii),
            color = "gray", alpha = 0.5) +
  geom_point(aes(x = age, y = circumference))
```

simulate_lme*Simulate values from an object of class lme***Description**

Simulate values from an object of class `lme`. Unequal variances, as modeled using the ‘weights’ option are supported, and there is experimental code for considering the ‘correlation’ structure.

Usage

```
simulate_lme(
  object,
  nsim = 1,
  psim = 1,
  value = c("matrix", "data.frame"),
  data = NULL,
  ...
)
```

Arguments

<code>object</code>	object of class <code>lme</code> or <code>gls</code>
<code>nsim</code>	number of samples, default 1
<code>psim</code>	parameter simulation level, 0: for fitted values, 1: for simulation from fixed parameters (assuming a fixed vcov matrix), 2: for simulation considering the uncertainty in the residual standard error (sigma), this returns data which will appear similar to the observed values. 3: in addition samples a new set of random effects.
<code>value</code>	whether to return a matrix (default) or an augmented data frame
<code>data</code>	the data argument is needed when using this function inside user defined functions.
...	additional arguments (it is possible to supply a newdata this way)

Details

This function is based on `predict.lme` function

It uses function `mvrnorm` to generate new values for the coefficients of the model using the Variance-Covariance matrix `vcov`. This variance-covariance matrix refers to the one for the parameters ‘beta’, not the one for the residuals.

Value

It returns a vector with simulated values with length equal to the number of rows in the original data

Note

I find the simulate.merMod in the lme4 pacakge confusing. There is use.u and several versions of re.form. From the documentation it seems that if use.u = TRUE, then the current values of the random effects are used. This would mean that it is equivalent to psim = 2 in this function. Then use.u = FALSE, would be equivalent to psim = 3. re.form allows for specifying the formula of the random effects.

See Also

[predict.lme](#) and ‘simulate.merMod’ in the ‘lme4’ package.

Examples

```
require(nlme)
data(Orange)

fm1 <- lme(circumference ~ age, random = ~ 1 | Tree, data = Orange)

sims <- simulate_lme(fm1, nsim = 10)
```

simulate_nlme

Simulate samples from a nonlinear mixed model from fixed effects

Description

Simulate multiple samples from a nonlinear model

Usage

```
simulate_nlme(
  object,
  nsim = 1,
  psim = 1,
  value = c("matrix", "data.frame"),
  data = NULL,
  ...
)
```

Arguments

object	object of class <code>gnls</code> or <code>nlme</code>
nsim	number of samples, default 1
psim	simulation level for fixed and random parameters see <code>simulate_nlme_one</code> for more details.
value	whether to return a matrix (default) or an augmented data frame
data	the data argument is needed when using this function inside user defined functions.
...	additional arguments to be passed to either <code>simulate_gnls</code> or <code>simulate_nlme_one</code>

Details

The details can be found in either `simulate_gnls` or `simulate_nlme_one`. This function is very simple and it only sets up a matrix and a loop in order to simulate several instances of model outputs.

Value

It returns a matrix with simulated values from the original object with number of rows equal to the number of rows of `fitted` and number of columns equal to the number of simulated samples ('nsim'). In the case of 'data.frame' it returns an augmented data.frame, which can potentially be a very large object, but which makes further plotting more convenient.

Examples

```
require(nlme)
data(barley, package = "nlraa")
barley2 <- subset(barley, year < 1974)
fit.lp.gnls2 <- gnls(yield ~ SSlinp(NF, a, b, xs), data = barley2)
barley2$year.f <- as.factor(barley2$year)
cfs <- coef(fit.lp.gnls2)
fit.lp.gnls3 <- update(fit.lp.gnls2,
                       params = list(a + b + xs ~ year.f),
                       start = c(cfs[1], 0, 0, 0,
                                 cfs[2], 0, 0, 0,
                                 cfs[3], 0, 0, 0))

sims <- simulate_nlme(fit.lp.gnls3, nsim = 3)
```

`simulate_nlme_one` *Simulate fitted values from an object of class `nlme`*

Description

This function is based on `predict.nlme` function

Usage

```
simulate_nlme_one(
  object,
  psim = 1,
  level = Q,
  asList = FALSE,
  na.action = na.fail,
  naPattern = NULL,
  data = NULL,
  ...
)
```

Arguments

object	object of class nlme
psim	parameter simulation level, 0: for fitted values, 1: for simulation from fixed parameters (assuming a fixed vcov matrix), 2: for simulation considering the residual error (sigma), this returns data which will appear similar to the observed values. Currently, working on psim = 3, which will simulate a new set of random effects. This can be useful when computing prediction intervals at the subject-level.
level	level at which simulations are performed. See predict.nlme . An important difference is that for this function multiple levels are not allowed.
asList	optional logical value. See predict.nlme
na.action	missing value action. See predict.nlme
naPattern	missing value pattern. See predict.nlme
data	the data argument is needed when using this function inside user defined functions.
...	additional arguments to be passed (possible to pass newdata this way)

Details

It uses function [mvrnorm](#) to generate new values for the coefficients of the model using the Variance-Covariance matrix [vcov](#)

Value

This function should return a vector with the same dimensions as the original data, unless newdata is provided.

simulate_nls*Simulate fitted values from an object of class [nls](#)*

Description

Simulate values from an object of class [nls](#).

Usage

```
simulate_nls(
  object,
  nsim = 1,
  psim = 1,
  resid.type = c("none", "resample", "normal", "wild"),
  value = c("matrix", "data.frame"),
  data = NULL,
  ...
)
```

Arguments

<code>object</code>	object of class nls
<code>nsim</code>	number of simulations to perform
<code>psim</code>	parameter simulation level, 0: for fitted values, 1: for simulation from fixed parameters (assuming a fixed vcov matrix), 2: simulation from sampling both from the parameters and the residuals, 3: for simulation considering the uncertainty in the residual standard error only (sigma) and fixing the parameter estimates at their original value; this will result in simulations similar to the observed values.
<code>resid.type</code>	either ‘none’, ‘resample’, ‘normal’ or ‘wild’.
<code>value</code>	either ‘matrix’ or ‘data.frame’
<code>data</code>	the data argument is needed when using this function inside user defined functions.
<code>...</code>	additional arguments (it is possible to supply a newdata this way)

Details

This function is based on [predict.gnls](#) function

It uses function [mvrnorm](#) to generate new values for the coefficients of the model using the Variance-Covariance matrix [vcov](#). This variance-covariance matrix refers to the one for the parameters ‘beta’, not the one for the residuals.

Value

It returns a vector with simulated values with length equal to the number of rows in the original data

Note

The default behavior is that simulations are performed for the mean function only. When ‘psim = 2’ this function will silently choose ‘resample’ as the ‘resid.type’. This is not ideal design for this function, but I made this choice for compatibility with other types of simulation originating from `glm` and `gam`.

See Also

[predict.gnls](#), [predict_nls](#)

Examples

```
data(barley, package = "nlraa")

fit <- nls(yield ~ SSlinp(NF, a, b, xs), data = barley)

sim <- simulate_nls(fit, nsim = 100)
```

sm

Sorghum and Maize growth in Greece

Description

Sorghum and Maize growth in Greece

Usage

sm

Format

A data frame with 235 rows and 5 columns

DOY -integer- Day of the year 141-303

Block -integer- Block in the experimental design 1-4

Input -integer- Input level 1 (Low) or 2 (High)

Crop -factor- either F (Fiber Sorghum), M (Maize), S (Sweet Sorghum)

Yield -numeric- Biomass yield in Mg/ha

Details

A dataset containing growth data for sorghum and maize in Greece.

Danalatos, N.G., S.V. Archontoulis, and K. Tsiboukas. 2009. Comparative analysis of sorghum versus corn growing under optimum and under water/nitrogen limited conditions in central Greece. In: From research to industry and markets: Proceedings of the 17th European Biomass Conference, Hamburg, Germany. 29 June–3 July 2009. ETA–Renewable Energies, Florence, Italy. p. 538–544.

Source

See above reference. (Currently available on ResearchGate).

SSagauss

self start for an asymmetric Gaussian bell-shaped curve

Description

Self starter for a type of bell-shaped curve

Usage

```
agauss(x, eta, beta, delta, sigma1, sigma2)
```

```
SSagauss(x, eta, beta, delta, sigma1, sigma2)
```

Arguments

x	input vector
eta	maximum value of y
beta	parameter controlling the lower values
delta	break-point separating the first and second half-bell curve
sigma1	scale for the first half
sigma2	scale for the second half

Details

This function is described in (doi:10.3390/rs12050827).

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 agauss: vector of the same length as x using an asymmetric bell-shaped Gaussian curve

Examples

```
require(ggplot2)
set.seed(1234)
x <- 1:30
y <- agauss(x, 10, 2, 10, 2, 6) + rnorm(length(x), 0, 0.02)
dat <- data.frame(x = x, y = y)
fit <- minpack.lm::nlsLM(y ~ SSagauss(x, eta, beta, delta, sigma1, sigma2), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SSbell	<i>self start for a bell-shaped curve</i>
--------	---

Description

Self starter for a type of bell-shaped curve

Usage

```
bell(x, ymax, a, b, xc)
```

```
SSbell(x, ymax, a, b, xc)
```

Arguments

x	input vector
ymax	maximum value of y
a	parameter controlling the spread (associated with a quadratic term)
b	parameter controlling the spread (associated with a cubic term)
xc	centering parameter

Details

This function is described in Archontoulis and Miguez (2015) - [doi:10.2134/agronj2012.0506](https://doi.org/10.2134/agronj2012.0506). One example application is Hammer et al. (2009) [doi:10.2135/cropsci2008.03.0152](https://doi.org/10.2135/cropsci2008.03.0152).

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 bell: vector of the same length as x using a bell-shaped curve

Examples

```
require(ggplot2)
set.seed(1234)
x <- 1:20
y <- bell(x, 8, -0.0314, 0.000317, 13) + rnorm(length(x), 0, 0.5)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSbell(x, ymax, a, b, xc), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SSbeta5*self start for Beta 5-parameter function***Description**

Self starter for Beta 5-parameter function

Usage

```
beta5(temp, mu, tb, a, tc, b)
SSbeta5(temp, mu, tb, a, tc, b)
```

Arguments

<code>temp</code>	input vector which is normally ‘temperature’
<code>mu</code>	mu parameter (see equation)
<code>tb</code>	base (low) temperature at which no expansion occurs
<code>a</code>	parameter describing the initial increasing phase
<code>tc</code>	critical (high) temperature at which no expansion occurs
<code>b</code>	parameter describing the decreasing phase

Details

For details see the publication by Yin et al. (1995) “A nonlinear model for crop development as a function of temperature ”. Agricultural and Forest Meteorology 77 (1995) 1-16

The form of the equation is:

$$\exp(mu) * (temp - tb)^a * (tc - temp)^b$$

Value

`beta5`: vector of the same length as `x` (`temp`) using the `beta5` function

Examples

```
require(minpack.lm)
require(ggplot2)
## Temperature response example
data(maizeleafext)
## Fit model
fit <- nlsLM(rate ~ SSbeta5(temp, mu, tb, a, tc, b), data = maizeleafext)
## Visualize
ndat <- data.frame(temp = 0:45)
ndat$rate <- predict(fit, newdata = ndat)
```

```
ggplot() +
  geom_point(data = maizeleafext, aes(temp, rate)) +
  geom_line(data = ndat, aes(x = temp, y = rate))
```

SSbg4rp

self start for the reparameterized Beta growth function with four parameters

Description

Self starter for Beta Growth function with parameters w.max, lt.e, ldtm, ldtb

Usage

```
bg4rp(time, w.max, lt.e, ldtm, ldtb)
SSbg4rp(time, w.max, lt.e, ldtm, ldtb)
```

Arguments

time	input vector (x) which is normally ‘time’, the smallest value should be close to zero.
w.max	value of weight or mass at its peak
lt.e	log of the time at which the maximum weight or mass has been reached.
ldtm	log of the difference between time at which the weight or mass reaches its peak and half its peak.
ldtb	log of the difference between time at which the weight or mass reaches its peak and when it starts growing

Details

For details see the publication by Yin et al. (2003) “A Flexible Sigmoid Function of Determinate Growth”. This is a reparameterization of the beta growth function (4 parameters) with guaranteed constraints, so it is expected to behave numerically better than [SSbgf4](#).

Reparameterizing the four parameter beta growth

- $ldtm = \log(t.e - t.m)$
- $ldtb = \log(t.m - t.b)$
- $t.e = \exp(lt.e)$
- $t.m = \exp(lt.e) - \exp(ldtm)$
- $t.b = (\exp(lt.e) - \exp(ldtm)) - \exp(ldtb)$

The form of the equation is:

$$w.max * (1 + (exp(lt.e) - time) / exp(ldtm)) * ((time - (exp(lt.e) - exp(ldtb))) / exp(ldtb))^{(exp(ldtb) / exp(ldtm))}$$

This is a reparameterized version of the Beta-Growth function in which the parameters are unconstrained, but they are expressed in the log-scale.

Value

`bg4rp`: vector of the same length as `x` (time) using the beta growth function with four parameters

Examples

```
require(ggplot2)
set.seed(1234)
x <- 1:100
y <- bg4rp(x, 20, log(70), log(30), log(20)) + rnorm(100, 0, 1)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSbg4rp(x, w.max, t.e, ldtm, ldtb), data = dat)
## We are able to recover the original values
exp(coef(fit)[2:4])
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SSbgf

*self start for Beta Growth Function***Description**

Self starter for Beta Growth function with parameters `w.max`, `t.m` and `t.e`

Usage

```
bgf(time, w.max, t.e, t.m)
SSbgf(time, w.max, t.e, t.m)
bgf2(time, w.max, w.b, t.e, t.m, t.b)
```

Arguments

<code>time</code>	input vector (<code>x</code>) which is normally ‘time’, the smallest value should be close to zero.
<code>w.max</code>	value of weight or mass at its peak
<code>t.e</code>	time at which the weight or mass reaches its peak.
<code>t.m</code>	time at which half of the maximum weight or mass has been reached.
<code>w.b</code>	weight or biomass at initial time
<code>t.b</code>	initial time offset

Details

For details see the publication by Yin et al. (2003) “A Flexible Sigmoid Function of Determinate Growth”.

The form of the equation is:

$$w.\max * (1 + (t.e - time)/(t.e - t.m)) * (time/t.e)^{(t.e/(t.e - t.m))}$$

. Given this function weight is expected to decay and reach zero again at $2 * t.e - t.m$.

Value

`bfg`: vector of the same length as `x` (time) using the beta growth function

`bfg2`: a numeric vector of the same length as `x` (time) containing parameter estimates for equation specified

Examples

```
## See extended example in vignette 'nlraa-AgronJ-paper'
x <- seq(0, 17, by = 0.25)
y <- bfg(x, 5, 15, 7)
plot(x, y)
```

SSbgf4

self start for Beta growth function with four parameters

Description

Self starter for Beta Growth function with parameters `w.max`, `t.e`, `t.m` and `t.b`

Usage

```
bfg4(time, w.max, t.e, t.m, t.b)
SSbgf4(time, w.max, t.e, t.m, t.b)
```

Arguments

<code>time</code>	input vector (<code>x</code>) which is normally ‘time’.
<code>w.max</code>	value of weight or mass at its peak.
<code>t.e</code>	time at which the weight or mass reaches its peak.
<code>t.m</code>	time at which half of the maximum weight or mass has been reached.
<code>t.b</code>	time at which growth starts.

Details

For details see the publication by Yin et al. (2003) “A Flexible Sigmoid Function of Determinate Growth”. This is a difficult function to fit because the linear constraints are not explicitly introduced in the optimization process. See function `SSbgrp` for a reparameterized version.

This is equation 11 (pg. 368) in the publication by Yin, but with correction (<https://doi.org/10.1093/aob/mcg091>) and with ‘w.b’ equal to zero.

Value

a numeric vector of the same length as x (time) containing parameter estimates for equation specified

`bgrf4`: vector of the same length as x (time) using the beta growth function with four parameters

Examples

```
data(sm)
## Let's just pick one crop
sm2 <- subset(sm, Crop == "M")
fit <- nls(Yield ~ SSbgrf4(DOY, w.max, t.e, t.m, t.b), data = sm2)
plot(Yield ~ DOY, data = sm2)
lines(sm2$DOY,fitted(fit))
## For this particular problem it could be better to 'fix' t.b and w.b
fit0 <- nls(Yield ~ bgrf2(DOY, w.max, w.b = 0, t.e, t.m, t.b = 141),
            data = sm2, start = list(w.max = 16, t.e= 240, t.m = 200))

x <- seq(0, 17, by = 0.25)
y <- bgrf4(x, 20, 15, 10, 2)
plot(x, y)
```

`SSbgrp`

self start for the reparameterized Beta growth function

Description

Self starter for Beta Growth function with parameters w.max, lt.m and ldt

Usage

```
bgrp(time, w.max, lt.e, ldt)
SSbgrp(time, w.max, lt.e, ldt)
```

Arguments

<code>time</code>	input vector (x) which is normally ‘time’, the smallest value should be close to zero.
<code>w.max</code>	value of weight or mass at its peak

lt.e	log of the time at which the maximum weight or mass has been reached.
ldt	log of the difference between time at which the weight or mass reaches its peak and half its peak ($\log(t.e - t.m)$).

Details

For details see the publication by Yin et al. (2003) “A Flexible Sigmoid Function of Determinate Growth”. This is a reparameterization of the beta growth function with guaranteed constraints, so it is expected to behave numerically better than [SSbgf](#).

The form of the equation is:

$$w.\max * (1 + (\exp(lt.e) - time)/\exp(ldt)) * (time/\exp(lt.e))^{\exp(lt.e)/\exp(ldt)}$$

. Given this function weight is expected to decay and reach zero again at $2 * ldt$. This is a reparameterized version of the Beta-Growth function in which the parameters are unconstrained, but they are expressed in the log-scale.

Value

bgrp: vector of the same length as x (time) using the beta growth function (reparameterized).

Note

In a few tests it seems that zero values of ‘time’ can cause the error message ‘NA/Nan/Inf in foreign function call (arg 1)’, so it might be better to remove them before running this function.

Examples

```
require(ggplot2)
x <- 1:30
y <- bgrp(x, 20, log(25), log(5)) + rnorm(30, 0, 1)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSbgrp(x, w.max, lt.e, ldt), data = dat)
## We are able to recover the original values
exp(coef(fit)[2:3])
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

Description

Self starter for a bilinear function with parameters a (intercept), b (first slope), xs (break-point), c (second slope)

Usage

```
blin(x, a, b, xs, c)
SSblin(x, a, b, xs, c)
```

Arguments

x	input vector
a	the intercept
b	the first-phase slope
xs	break-point of transition between first-phase linear and second-phase linear
c	the second-phase slope

Details

This is a special case with just two parts but a more general approach is to consider a segmented function with several breakpoints and linear segments. Splines would be even more general. Also this model assumes that there is a break-point that needs to be estimated.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 blin: vector of the same length as x using the bilinear function

See Also

package **segmented**.

Examples

```
require(ggplot2)
set.seed(1234)
x <- 1:30
y <- blin(x, 0, 0.75, 15, 1.75) + rnorm(30, 0, 0.5)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSblin(x, a, b, xs, c), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
## Minimal example
## This is probably about the smallest dataset you
## should use with this function
dat2 <- data.frame(x = 1:5, y = c(1.1, 1.9, 3.1, 2, 0.9))
fit2 <- nls(y ~ SSblin(x, a, b, xs, c), data = dat2)
ggplot(data = dat2, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit2)))
```

<code>SScard3</code>	<i>self start for cardinal temperature response</i>
----------------------	---

Description

Self starter for cardinal temperature response function

Usage

```
card3(x, tb, to, tm)
```

```
SScard3(x, tb, to, tm)
```

Arguments

<code>x</code>	input vector (<code>x</code>) which is normally ‘temperature’.
<code>tb</code>	base temperature
<code>to</code>	optimum temperature
<code>tm</code>	maximum temperature

Details

This function is described in Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506)

Value

`card3`: vector of the same length as `x` using a `card3` function

Author(s)

Caio dos Santos and Fernando Miguez

Examples

```
## A temperature response function
require(ggplot2)
set.seed(1234)
x <- 1:50
y <- card3(x, 13, 25, 36) + rnorm(length(x), sd = 0.05)
dat1 <- data.frame(x = x, y = y)
fit1 <- nls(y ~ SScard3(x, tb, to, tm), data = dat1)

ggplot(data = dat1, aes(x, y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit1)))
```

SSdlf*self start for Declining Logistic Function***Description**

Self starter for declining logistic function with parameters asym, a2, xmid and scal

Usage

```
dlf(time, asym, a2, xmid, scal)
SSdlf(time, asym, a2, xmid, scal)
```

Arguments

time	input vector (x) which is normally ‘time’, the smalles value should be close to zero.
asym	value of weight or mass at its peak (maximum)
a2	value of weight or mass at its trough (minimum)
xmid	time at which half of the maximum weight or mass has bean reached.
scal	scale parameter which controls the spread also interpreted in terms of time to go from xmid to approx. 0.63 asym

Details

Response function:

$$y = (\text{asym} - \text{a2}) / (1 + \exp((\text{xmid} - \text{time}) / \text{scal})) + \text{a2}$$

- asym: upper asymptote
- xmid: time when y is midway between w and a
- scal: controls the spread
- a2: lower asymptote

The four parameter logistic [SSfp1](#) is essentially equivalent to this function, but here the interpretation of the parameters is different and this is the form used in Oddi et. al. (2019) (see vignette).

Value

a numeric vector of the same length as x (time) containing parameter estimates for equation specified

dlf: vector of the same length as x (time) using the declining logistic function

Examples

```
## Extended example in the vignette 'nlraa-Oddi-LFMC'
x <- seq(0, 17, by = 0.25)
y <- dlf(x, 2, 10, 8, 1)
plot(x, y, type = "l")
```

SSexpf

self start for an exponential function

Description

Self starter for a simple exponential function

Usage

```
expf(x, a, c)
SSexpf(x, a, c)
```

Arguments

- x input vector (x)
- a represents the value at x = 0
- c represents the exponential rate

Details

This is the exponential function

$$y = a * \exp(c * x)$$

For more details see: Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506).

Value

- a numeric vector of the same length as x containing parameter estimates for equation specified
- expf: vector of the same length as x using the profd function

Examples

```
require(ggplot2)
set.seed(1234)
x <- 1:15
y <- expf(x, 10, -0.3) + rnorm(15, 0, 0.2)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSexpf(x, a, c), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
```

```
geom_point() +
geom_line(aes(y = fitted(fit)))
```

SSexpfp*self start for an exponential-plateau function***Description**

Self starter for an exponential-plateau function

Usage

```
expfp(x, a, c, xs)
```

```
SSexpfp(x, a, c, xs)
```

Arguments

x	input vector (x)
a	represents the value at x = 0
c	represents the exponential rate
xs	represents the breakpoint at which the plateau starts

Details

This is the exponential-plateau function, where ‘xs’ is the break-point

$$(x < xs) * a * \exp(c * x) + (x \geq xs) * (a * \exp(c * xs))$$

For more details see: Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506).

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
expfp: vector of the same length as x using the expfp function

Examples

```
require(ggplot2)
set.seed(12345)
x <- 1:30
y <- expfp(x, 10, 0.1, 15) + rnorm(30, 0, 1.5)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSexpfp(x, a, c, xs), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SSexplin	<i>self start for the exponential-linear growth equation</i>
----------	--

Description

Self starter for an exponential-linear growth equation

Usage

```
explin(t, cm, rm, tb)
```

```
SSexplin(t, cm, rm, tb)
```

Arguments

t	input vector (time)
cm	parameter related to the maximum growth during the linear phase
rm	parameter related to the maximum growth during the exponential phase
tb	time at which switch happens

Details

J. GOUDRIAAN, J. L. MONTEITH, A Mathematical Function for Crop Growth Based on Light Interception and Leaf Area Expansion, Annals of Botany, Volume 66, Issue 6, December 1990, Pages 695–701, doi:10.1093/oxfordjournals.aob.a088084

The equation is:

$$(cm/rm) * \log(1 + \exp(rm * (t - tb)))$$

This function is described in Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506).

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
explin: vector of the same length as x using a explin function

Examples

```
require(ggplot2)
set.seed(12345)
x <- seq(1,100, by = 5)
y <- explin(x, 20, 0.14, 30) + rnorm(length(x), 0, 5)
y <- abs(y)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSexplin(x, cm, rm, tb), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
```

```
geom_line(aes(y = fitted(fit)))
```

SSgmicmen

self start for a generalized Michaelis-Menten function

Description

Self starter for a Michealis-Menten function with parameters

Usage

```
gmicmen(x, y0, ymax, c, k)
```

```
SSgmicmen(x, y0, ymax, c, k)
```

Arguments

x	input vector
y0	the lowest value
ymax	the maximum value
c	parameter controlling the shape of the function
k	parameter controlling the time for maximum value

Details

This is a modification of an equation that appears in the paper in the details. # It is not clear how useful it is.

Source: A generalized Michaelis-Menten equation for the analysis of growth. Lopez et al. J. Anim. Sci. 2000. 78:1816-1828.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
gmicmen: vector of the same length as x using the modified Michaelis-Menten function

Examples

```
require(ggplot2)
set.seed(123)
x <- 1:30
y <- gmicmen(x, 1, 10, 0.7, 10) + rnorm(30, 0, 0.01)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSgmicmen(x, y0, ymax, c, k), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
```

```

geom_line(aes(y = fitted(fit)))
## Confidence intervals
confint(fit)

## Different value for c
y <- gmicmen(x, 1, 10, 5, 10) + rnorm(30, 0, 0.01)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSgmicmen(x, y0, ymax, c, k), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
## Confidence intervals
confint(fit)

```

SSharm1

self start for a harmonic regression model

Description

Self starter for a harmonic regression

Usage

```

harm1(x, b0, b1, cos1, sin1)

SSharm1(x, b0, b1, cos1, sin1)

```

Arguments

x	input vector
b0	intercept of the harmonic regression
b1	slope of the harmonic regression
cos1	coefficient associated with the cosine of the harmonic regression
sin1	coefficient associated with the sine of the harmonic regression

Details

Harmonic regression is actually a type of linear regression. Just adding it for convenience.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 harm1: vector of the same length as x using a harmonic regression

Examples

```
require(ggplot2)
set.seed(1234)
x <- seq(0, 3, length.out = 100)
y <- harm1(x, 0, 0, 0.05, 0) + rnorm(length(x), 0, 0.002)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSharm1(x, b0, b1, cos1, sin1), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SShill

self start for Hill Function

Description

Self starter for Hill function with parameters Ka, n and a

Usage

```
hill1(x, Ka)
SShill1(x, Ka)

hill2(x, Ka, n)
SShill2(x, Ka, n)

hill3(x, Ka, n, a)
SShill3(x, Ka, n, a)
```

Arguments

x	input vector (x). Concentration of substrate in the original Hill model.
Ka	parameter representing the concentration at which half of maximum y is attained
n	parameter which controls the curvature
a	parameter which controls the maximum value of the response (asymptote)

Details

For details see [https://en.wikipedia.org/wiki/Hill_equation_\(biochemistry\)](https://en.wikipedia.org/wiki/Hill_equation_(biochemistry))

The form of the equations are:

hill1:

$$1/(1 + (Ka/x))$$

hill2:

$$1/(1 + (Ka/x)^n)$$

hill3:

$$a/(1 + (Ka/x)^n)$$

Value

hill1: vector of the same length as x (time) using the Hill 1 function

hill2: vector of the same length as x (time) using the Hill 2 function

hill3: vector of the same length as x (time) using the Hill 3 function

Note

Zero values are not allowed.

Examples

```
require(ggplot2)
## Example for hill1
set.seed(1234)
x <- 1:20
y <- hill1(x, 10) + rnorm(20, sd = 0.03)
dat1 <- data.frame(x = x, y = y)
fit1 <- nls(y ~ SShill1(x, Ka), data = dat1)

## Example for hill2
y <- hill2(x, 10, 1.5) + rnorm(20, sd = 0.03)
dat2 <- data.frame(x = x, y = y)
fit2 <- nls(y ~ SShill2(x, Ka, n), data = dat2)

## Example for hill3
y <- hill3(x, 10, 1.5, 5) + rnorm(20, sd = 0.03)
dat3 <- data.frame(x = x, y = y)
fit3 <- nls(y ~ SShill3(x, Ka, n, a), data = dat3)

ggplot(data = dat3, aes(x, y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit3)))
```

sslinp*self start for linear-plateau function***Description**

Self starter for linear-plateau function with parameters a (intercept), b (slope), xs (break-point)

Usage

```
linp(x, a, b, xs)
```

```
SSlinp(x, a, b, xs)
```

Arguments

x	input vector
a	the intercept
b	the slope
xs	break-point of transition between linear and plateau

Details

This function is linear when $x < xs : (a + b*x)$ and flat ($asymptote = a + b*xs$) when $x \geq xs$.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified

linp: vector of the same length as x using the linear-plateau function

See Also

package **segmented**.

Examples

```
require(ggplot2)
set.seed(123)
x <- 1:30
y <- linp(x, 0, 1, 20) + rnorm(30, 0, 0.5)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSlinp(x, a, b, xs), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
## Confidence intervals
confint(fit)
```

SSlogis5	<i>self start for five-parameter logistic function</i>
----------	--

Description

Self starter for a five-parameter logistic function.

Usage

```
logis5(x, asym1, asym2, xmid, iscal, theta)
SSlogis5(x, asym1, asym2, xmid, iscal, theta)
```

Arguments

x	input vector (x)
asym1	asymptotic value for low values of x
asym2	asymptotic value for high values of x
xmid	value of x at which $y = (\text{asym1} + \text{asym2})/2$ (only when theta = 1)
iscal	steepness of transition from asym1 to asym2 (inverse of the scale)
theta	asymmetry parameter, if it is equal to 1, this is the four parameter logistic

Details

The equation for this function is:

$$f(x) = \text{asym2} + (\text{asym1} - \text{asym2}) / (1 + \exp(\text{ascal} * (\log(x) - \log(\text{xmid}))))^{\text{theta}}$$

This is known as the Richards' function or the log-logistic and it is described in Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506).

Value

a numeric vector of the same length as x (time) containing parameter estimates for equation specified

logis5: vector of the same length as x (time) using the 5-parameter logistic

Examples

```
require(ggplot2)
set.seed(1234)
x <- seq(0, 2000, 100)
y <- logis5(x, 35, 10, 800, 5, 2) + rnorm(length(x), 0, 0.5)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSlogis5(x, asym1, asym2, xmid, iscal, theta), data = dat)
## plot
```

```
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))

x <- seq(0, 2000)
y <- logis5(x, 30, 10, 800, 5, 2)
plot(x, y)
```

SSmoh

self start for modified hyperbola (photosynthesis)

Description

Self starter for modified Hyperbola with parameters: asym, xmin and k

Usage

```
moh(x, asym, xmin, k)

SSmoh(x, asym, xmin, k)
```

Arguments

x	input vector (x) which is normally a controlling variable such as nitrogen
asym	asymptotic value when x tends to infinity
xmin	value of x for which y equals zero
k	curvature parameter

Details

This function is described in Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506). See Table S3 (Eq. 3.8)

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 moh: vector of the same length as x (time) using the modified hyperbola

Examples

```
require(ggplot2)
set.seed(1234)
x <- seq(3, 30)
y <- moh(x, 35, 3, 0.83) + rnorm(length(x), 0, 0.5)
dat1 <- data.frame(x = x, y = y)
fit <- nls(y ~ SSmoh(x, asym, xmin, k), data = dat1)
## Visualize observed and simulated
ggplot(data = dat1, aes(x = x, y = y)) +
```

```

geom_point() +
  geom_line(aes(y = fitted(fit)))
## Testing predict function
prd <- predict_nls(fit, interval = "confidence")
dat1A <- cbind(dat1, prd)
## Plotting
ggplot(data = dat1A, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit))) +
  geom_ribbon(aes(ymin = Q2.5, ymax = Q97.5),
              fill = "purple", alpha = 0.3)

x <- seq(0, 20)
y <- moh(x, 30, 3, 0.9)
plot(x, y)

```

SSnrh

self start for non-rectangular hyperbola (photosynthesis)

Description

Self starter for Non-rectangular Hyperbola with parameters: asymptote, quantum efficiency, curvature and dark respiration

Usage

```

nrh(x, asym, phi, theta, rd)
SSnrh(x, asym, phi, theta, rd)

```

Arguments

x	input vector (x) which is normally light intensity (PPFD, Photosynthetic Photon Flux Density).
asym	asymptotic value for photosynthesis
phi	quantum efficiency (mol CO ₂ per mol of photons) or initial slope of the light response
theta	curvature parameter for smooth transition between limitations
rd	dark respiration or value of CO ₂ uptake at zero light levels

Details

This function is described in Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506).

Value

a numeric vector of the same length as x (time) containing parameter estimates for equation specified

nrh: vector of the same length as x (time) using the non-rectangular hyperbola

Examples

```

require(ggplot2)
set.seed(1234)
x <- seq(0, 2000, 100)
y <- nrh(x, 35, 0.04, 0.83, 2) + rnorm(length(x), 0, 0.5)
dat9 <- data.frame(x = x, y = y)
fit <- nls(y ~ SSnrh(x, asym, phi, theta, rd), data = dat9)
## Visualize observed and simulated
ggplot(data = dat9, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
## Testing predict function
prd <- predict_nls(fit, interval = "confidence")
dat9A <- cbind(dat9, prd)
## Plotting
ggplot(data = dat9A, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit))) +
  geom_ribbon(aes(ymin = Q2.5, ymax = Q97.5),
              fill = "purple", alpha = 0.3)

x <- seq(0, 2000)
y <- nrh(x, 30, 0.04, 0.85, 2)
plot(x, y)

```

SSpexpf

self start for plateau-exponential function

Description

Self starter for an plateau-exponential function

Usage

```
pexpf(x, a, xs, c)
```

```
SSpexpf(x, a, xs, c)
```

Arguments

x	input vector (x)
a	represents the value for the plateau
xs	represents the breakpoint at which the plateau ends
c	represents the exponential rate

Details

The equation is: $for x < xs : y = a and x \geq xs : a * exp(c * (x - xs))$.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 pexpf: vector of the same length as x using the pexpf function

Examples

```
require(ggplot2)
set.seed(1234)
x <- 1:30
y <- pexpf(x, 20, 15, -0.2) + rnorm(30, 0, 1)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSpexpf(x, a, xs, c), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SSplin

*self start for plateau-linear function***Description**

Self starter for plateau-linear function with parameters a (plateau), xs (break-point), b (slope)

Usage

```
plin(x, a, xs, b)
```

```
SSplin(x, a, xs, b)
```

Arguments

x	input vector
a	the initial plateau
xs	break-point of transition between plateau and linear
b	the slope

Details

Initial plateau with a second linear phase. When $x < xs : y = a$ and when $x \geq xs : y = a + b * (x - xs)$.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 plin: vector of the same length as x using the plateau-linear function

Examples

```
require(ggplot2)
set.seed(123)
x <- 1:30
y <- plin(x, 10, 20, 1) + rnorm(30, 0, 0.5)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSquad(x, a, xs, b), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
## Confidence intervals
confint(fit)
```

SSquad

self start for plateau-quadratic function

Description

Self starter for plateau-quadratic function with parameters a (plateau), xs (break-point), b (slope), c (quadratic)

Usage

```
pquad(x, a, xs, b, c)
```

```
SSquad(x, a, xs, b, c)
```

Arguments

x	input vector
a	the plateau value
xs	break-point of transition between plateau and quadratic
b	the slope (linear term)
c	quadratic term

Details

Reference for nonlinear regression Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506).

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 pquad: vector of the same length as x using the plateau-quadratic function

Examples

```
require(ggplot2)
set.seed(12345)
x <- 1:40
y <- pquad(x, 5, 20, 1.7, -0.04) + rnorm(40, 0, 0.6)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSquad(x, a, xs, b, c), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
confint(fit)
```

SSquad3

self start for plateau-quadratic function

Description

Self starter for plateau-quadratic function with (three) parameters a (intercept), b (slope), c (quadratic)

Usage

```
pquad3(x, a, b, c)
```

```
SSquad3(x, a, b, c)
```

Arguments

x	input vector
a	the intercept
b	the slope
c	quadratic term

Details

Reference for nonlinear regression Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506).

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 quadp: vector of the same length as x using the quadratic-plateau function

Examples

```
require(ggplot2)
require(minpack.lm)
set.seed(123)
x <- 1:30
y <- pquad3(x, 20.5, 0.36, -0.012) + rnorm(30, 0, 0.3)
dat <- data.frame(x = x, y = y)
fit <- nlsLM(y ~ SSquad3(x, a, b, c), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SSprof

self start for profile decay function

Description

Self starter for a decay of a variable within a canopy (e.g. nitrogen concentration).

Usage

```
prof(x, a, b, c, d)
SSprof(x, a, b, c, d)
```

Arguments

x	input vector (x)
a	represents the maximum value
b	represents the minimum value
c	represents the rate of decay
d	represents an empirical coefficient which provides flexibility

Details

This function is described in Archontoulis and Miguez (2015) - [doi:10.2134/agronj2012.0506](https://doi.org/10.2134/agronj2012.0506) and originally in Johnson et al. (2010) Annals of Botany 106: 735–749, 2010. [doi:10.1093/aob/mcq183](https://doi.org/10.1093/aob/mcq183).

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 profd: vector of the same length as x using the profd function

Examples

```

require(ggplot2)
set.seed(1234)
x <- 1:10
y <- profd(x, 0.3, 0.05, 0.5, 4) + rnorm(10, 0, 0.01)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSprof(x, a, b, c, d), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
## profiling
## It does not work at a lower alphamax level
## Use this if you want to look at all four parameters
## par(mfrow=c(2,2))
plot(profile(fit, alphamax = 0.016))
## Reset graphical parameter as appropriate: par(mfrow=c(1,1))
## parameter 'd' is not well constrained
confint(fit, level = 0.9)

```

SSquadp

self start for quadratic-plateau function

Description

Self starter for quadratic plateau function with parameters a (intercept), b (slope), c (quadratic), xs (break-point)

Usage

```
quadp(x, a, b, c, xs)
```

```
SSquadp(x, a, b, c, xs)
```

Arguments

x	input vector
a	the intercept
b	the slope
c	quadratic term
xs	break point of transition between quadratic and plateau

Details

Reference for nonlinear regression Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506).

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 quadp: vector of the same length as x using the quadratic-plateau function

Examples

```
require(ggplot2)
set.seed(123)
x <- 1:30
y <- quadp(x, 5, 1.7, -0.04, 20) + rnorm(30, 0, 0.6)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSquadp3(x, a, b, c, xs), data = dat, algorithm = "port")
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SSquadp3

*self start for quadratic-plateau function***Description**

Self starter for quadratic plateau function with (three) parameters a (intercept), b (slope), c (quadratic)

Usage

```
quadp3(x, a, b, c)
SSquadp3(x, a, b, c)
```

Arguments

x	input vector
a	the intercept
b	the slope
c	quadratic term

Details

The equation is, for a response (y) and a predictor (x):
 $y (x \leq xs) * (a + b * x + c * x^2) + (x > xs) * (a + (-b^2)/(4 * c))$

where the break-point (xs) is $-0.5 * b / c$
 and the asymptote is $(a + (-b^2)/(4 * c))$

In this model the parameter 'xs' is not directly estimated. If this is required, the model 'SSquadp3xs' should be used instead.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 quadp: vector of the same length as x using the quadratic-plateau function

Examples

```
require(ggplot2)
set.seed(123)
x <- 1:30
y <- quadp3(x, 5, 1.7, -0.04) + rnorm(30, 0, 0.6)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSquadp3(x, a, b, c), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SSquadp3xs

self start for quadratic-plateau function (xs)

Description

Self starter for quadratic plateau function with (three) parameters a (intercept), b (slope), xs (break-point)

Usage

```
quadp3xs(x, a, b, xs)
SSquadp3xs(x, a, b, xs)
```

Arguments

x	input vector
a	the intercept
b	the slope
xs	break-point

Details

The equation is, for a response (y) and a predictor (x):

$$y (x \leq xs) * (a + b * x + (-0.5 * b/xs) * x^2) + (x > xs) * (a + (b^2)/(-2 * b/xs))$$

where the quadratic term is (c) is $-0.5 * b/xs$
 and the asymptote is $(a + (b^2)/(4 * c))$.

This model does not estimate the quadratic parameter ‘c’ directly. If this is required, the model ‘SSquadp3’ should be used instead.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 quadp3xs: vector of the same length as x using the quadratic-plateau function

Examples

```
require(ggplot2)
set.seed(123)
x <- 1:30
y <- quadp3xs(x, 5, 1.7, 20) + rnorm(30, 0, 0.6)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSquadp3xs(x, a, b, xs), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

SSquadpq

*self start for quadratic-plateau-quadratic (QPQ) function***Description**

Self starter for quadratic plateau function with (four) parameters a (intercept), b (slope), xs (break-point), ldxs (log of the difference between break-point and second break-point)

Usage

```
quadpq(x, a, b, xs, ldxs)
SSquadpq(x, a, b, xs, ldxs)
```

Arguments

x	input vector
a	the intercept
b	the slope
xs	first break-point
ldxs	log of the difference between break-point and second break-point

Details

The equation is, for a response (y) and a predictor (x):

$$y = (x \leq xs) * (a + b*x + (-0.5*b/xs)*x^2) + (x > xs \& x \leq (xs+dxs)) * (a + (-b^2)/(4*(-0.5*b/xs))) + (x > (xs+dxs)) * (a + (-b^2)/(4*(-0.5*b/xs)))$$

This is a somewhat complicated equation. The interpretation of the parameters are simple. The model is parameterized in terms of the log of dxs (or ldxs). The parameter is ensured to be positive by taking the exponential.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
quadpq: vector of the same length as x using the quadratic-plateau-quadratic function

Examples

```
require(ggplot2)
set.seed(123)
x <- 0:25
y <- quadpq(x, 1, 0.5, 10, 1.5) + rnorm(length(x), 0, 0.3)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSquadpq(x, a, b, xs, dxs), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit))) +
  geom_vline(aes(xintercept = coef(fit)[3]), linetype = 2) +
  geom_vline(aes(xintercept = coef(fit)[3] + exp(coef(fit)[4])), linetype = 3)
```

SSratio

self start for a rational curve

Description

Self starter for a rational curve

Usage

```
ratio(x, a, b, c, d)
SSratio(x, a, b, c, d)
```

Arguments

x	input vector
a	parameter related to the maximum value of the response (numerator)
b	power exponent for numerator
c	parameter related to the maximum value of the response (denominator)
d	power exponent for denominator

Details

The equation is:

$$a * x^c / (1 + b * x^d)$$

This function is described in Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506). One example application is in Bril et al. (1994) <https://edepot.wur.nl/333930> - pages 19 and 21. The parameters are difficult to interpret, but the function is very flexible. I have not tested this, but it might be beneficial to re-scale x and y to the (0,1) range if this function is hard to fit. https://en.wikipedia.org/wiki/Rational_function.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified

ratio: vector of the same length as x using a rational function

Examples

```
require(ggplot2)
require(minpack.lm)
set.seed(1234)
x <- 1:100
y <- ratio(x, 1, 0.5, 1, 1.5) + rnorm(length(x), 0, 0.025)
dat <- data.frame(x = x, y = y)
fit <- nlsLM(y ~ SSratio(x, a, b, c, d), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

Description

Self starter for Ricker function with parameters a and b

Usage

```
 ricker(time, a, b)
 SSricker(time, a, b)
```

Arguments

time	input vector (x) which is normally ‘time’, the smallest value should be close to zero.
a	which is related to the initial growth slope
b	which is related to the slowing down or decline

Details

This function is described in Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506) and originally in Ricker, W. E. (1954) Stock and Recruitment Journal of the Fisheries Research Board of Canada, 11(5): 559–623. (doi:10.1139/f54-039). The equation is: $a * time * \exp(-b * time)$.

Value

a numeric vector of the same length as x (time) containing parameter estimates for equation specified

ricker: vector of the same length as x (time) using the ricker function

Examples

```
require(ggplot2)
set.seed(123)
x <- 1:30
y <- 30 * x * exp(-0.3 * x) + rnorm(30, 0, 0.25)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSricker(x, a, b), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
```

Description

Self starter for smooth cardinal temperature response function

Usage

```
scard3(x, tb, to, tm, curve = 2)

SSscard3(x, tb, to, tm, curve = 2)
```

Arguments

x	input vector (x) which is normally ‘temperature’.
tb	base temperature
to	optimum temperature
tm	maximum temperature
curve	curvature (default is 2)

Details

An example application can be found in (doi:10.1016/j.envsoft.2014.04.009)

This function is described in Archontoulis and Miguez (2015) - (doi:10.2134/agronj2012.0506) - Equation 5.1 in Table 1.

Value

scard3: vector of the same length as x using a scard3 function

Author(s)

Caio dos Santos and Fernando Miguez

Examples

```
## A temperature response function
require(ggplot2)
set.seed(1234)
x <- 1:50
y <- scard3(x, 13, 25, 36) + rnorm(length(x), sd = 0.05)
dat1 <- data.frame(x = x, y = y)
fit1 <- nls(y ~ SSscard3(x, tb, to, tm), data = dat1)

ggplot(data = dat1, aes(x, y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit1)))
```

SSsharp

self start for temperature response

Description

Self starter for temperature response function

Usage

```
sharp(temp, r_tref, e, el, tl, eh, th, tref = 25)
```

```
SSsharp(temp, r_tref, e, el, tl, eh, th, tref = 25)
```

Arguments

temp	input vector (x) which is normally ‘temperature’.
r_tref	rate at the standardised temperature, tref
e	activation energy (eV)
el	low temperature de-activation energy (eV)
tl	temperature at which the enzyme is half active and half suppressed due to low temperatures
eh	high temperature de-activation energy (eV)
th	temperature at which enzyme is half active and half suppressed due to high temperatures
tref	standardisation temperature in degrees centigrade. Temperature at which rates are not inactivated by either high or low temperatures. Typically, 25 degrees.

Details

For details see Schoolfield, R. M., Sharpe, P. J. & Magnuson, C. E. Non-linear regression of biological temperature-dependent rate models based on absolute reaction-rate theory. Journal of Theoretical Biology 88, 719-731 (1981)

Value

sharp: vector of the same length as x using a sharp function

Note

I do not recommend using this function.

Examples

```

require(ggplot2)
require(minpack.lm)

temp <- 0:45
rate <- sharp(temp, 1, 0.03, 1.44, 28, 19, 44) + rnorm(length(temp), 0, 0.05)
dat <- data.frame(temp = temp, rate = rate)
## Fit model
fit <- nlsLM(rate ~ SSsharp(temp, r_tref, e, el, tl, eh, th, tref = 20), data = dat)
## Visualize
ggplot(data = dat, aes(temp, rate)) + geom_point() + geom_line(aes(y = fitted(fit)))

```

SSspherical

self start for spherical function

Description

Self starter for a spherical function with parameters a (intercept), b (see below), xs (break-point)

Usage

```

spherical(x, a, b, xs)
SSspherical(x, a, b, xs)

```

Arguments

x	input vector
a	the intercept
b	the difference between the intercept and the asymptote, so that $a + b = \text{asymptote}$
xs	break-point of transition between nonlinear and plateau

Details

This equation was found in a publication by Dobermann et al. (2011) [doi:10.2134/agronj2010.0179](https://doi.org/10.2134/agronj2010.0179)

This function is nonlinear when $x < xs$ and flat ($\text{asymptote} = a + b$) when $x \geq xs$.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 spherical: vector of the same length as x using the spherical function

Examples

```
require(ggplot2)
set.seed(123)
x <- seq(0, 400, length.out = 50)
y <- spherical(x, 2, 5, 200) + rnorm(length(x), sd = 0.5)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SSspherical(x, a, b, xs), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
## Confidence intervals
confint(fit)
```

SStemp3

self start for Collatz temperature response

Description

Self starter for Collatz temperature response function

Usage

```
temp3(x, t.m, t.l, t.h)
SStemp3(x, t.m, t.l, t.h)
```

Arguments

x	input vector (x) which is normally ‘temperature’.
t.m	medium temperature
t.l	low temperature
t.h	high temperature

Details

Collatz GJ , Ribas-Carbo M Berry JA (1992) Coupled Photosynthesis-Stomatal Conductance Model for Leaves of C4 Plants. Functional Plant Biology 19, 519-538. <https://doi.org/10.1071/PP9920519>

Value

temp3: vector of the same length as x using a temp function

Examples

```
## A temperature response function
require(ggplot2)
set.seed(1234)
x <- 1:50
y <- temp3(x, 25, 13, 36) + rnorm(length(x), sd = 0.05)
dat1 <- data.frame(x = x, y = y)
fit1 <- nls(y ~ SStemp3(x, t.m, t.l, t.h), data = dat1)

ggplot(data = dat1, aes(x, y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit1)))
```

SStrlin

self start for a trilinear Function

Description

Self starter for a tri-linear function with parameters a (intercept), b (first slope), xs1 (first break-point), c (second slope), xs2 (second break-point) and d (third slope)

Usage

```
trlin(x, a, b, xs1, c, xs2, d)
SStrlin(x, a, b, xs1, c, xs2, d)
```

Arguments

x	input vector
a	the intercept
b	the first-phase slope
xs1	first break-point of transition between first-phase linear and second-phase linear
c	the second-phase slope
xs2	second break-point of transition between second-phase linear and third-phase linear
d	the third-phase slope

Details

This is a special case with just three parts (and two break points) but a more general approach is to consider a segmented function with several breakpoints and linear segments. Splines would be even more general. Also this model assumes that there are two break-points that needs to be estimated. The guess for the initial values splits the dataset in half, so it this will work when one break-point is in the first half and the second is in the second half.

Value

a numeric vector of the same length as x containing parameter estimates for equation specified
 trlin: vector of the same length as x using the tri-linear function

See Also

package **segmented**.

Examples

```
require(ggplot2)
set.seed(1234)
x <- 1:30
y <- trlin(x, 0.5, 2, 10, 0.1, 20, 1.75) + rnorm(30, 0, 0.5)
dat <- data.frame(x = x, y = y)
fit <- nls(y ~ SStrlin(x, a, b, xs1, c, xs2, d), data = dat)
## plot
ggplot(data = dat, aes(x = x, y = y)) +
  geom_point() +
  geom_line(aes(y = fitted(fit)))
## Minimal example
## This is probably about the smallest dataset you
## should use with this function
dat2 <- data.frame(x = 1:8, y = c(1.1, 1.9, 3.1, 2.5, 1.4, 0.9, 2.2, 2.9))
fit2 <- nls(y ~ SStrlin(x, a, b, xs1, c, xs2, d), data = dat2)
## expandin for plotting
ndat <- data.frame(x = seq(1, 8, by = 0.1))
ndat$prd <- predict(fit2, newdata = ndat)
ggplot() +
  geom_point(data = dat2, aes(x = x, y = y)) +
  geom_line(data = ndat, aes(x = x, y = prd))
```

summary_simulate

Summarize a matrix of simulations by their mean (median), sd (mad), and quantiles

Description

Utility function to summarize the output from ‘simulate’ functions in this package

Usage

```
summary_simulate(
  object,
  probs = c(0.025, 0.975),
  robust = FALSE,
```

```

  data,
  by,
  na.rm = FALSE,
  ...
)

```

Arguments

<code>object</code>	nobs x nsim matrix where nobs are the number of observations in the dataset and nsim are the number of simulations
<code>probs</code>	the percentiles to be computed by the quantile function
<code>robust</code>	If FALSE (the default) the mean is used as the measure of central tendency and the standard deviation as the measure of variability. If TRUE, the median and the median absolute deviation (MAD) are applied instead.
<code>data</code>	the original data.frame used to fit the model. A data.frame will be returned instead of a matrix in this case.
<code>by</code>	optionally aggregate the results by some factor in the data.frame. It will be coerced to a formula. This should either be a character or a formula (starting with ‘~’). The aggregation follows the ‘robust’ argument above.
<code>na.rm</code>	whether to remove missing values (default is FALSE).
...	additional arguments to be passed. (none used at the moment)

Value

By default it returns a matrix unless the ‘data’ argument is present and then it will return a data.frame

Examples

```

data(barley, package = "nlraa")
fit <- nls(yield ~ SSlinp(NF, a, b, xs), data = barley)
sim <- simulate_nls(fit, nsim = 100)
sims <- summary_simulate(sim)

## If we want to combine the data.frame
simd <- summary_simulate(sim, data = barley)
## If we also want to aggregate by nitrogen rate
simda <- summary_simulate(sim, data = barley, by = "NF")
## The robust option uses the median instead
simdar <- summary_simulate(sim, data = barley, by = "NF",
                           robust = TRUE)

```

`swpg`

Water limitations for Soybean growth

Description

Simulated data based on observed data presented in Sinclair (1986) - Fig. 1A

Usage

`swpg`

Format

A data frame with 20 rows and 3 columns

ftsw Fraction of Transpirable Soil Water (0-1)

lfgt Relative Leaf Growth scaled from 0 to 1

Details

Sinclair, T.R. Water and Nitrogen Limitations in Soybean Grain Production I. Model Development. Field Crops Research. 125-141.

Source

Simulated data (much cleaner than original) based on the above publication

`var_cov`

Variance Covariance matrix of for g(n)ls and (n)lme models

Description

Extracts the variance covariance matrix (residuals, random or all)

Usage

```
var_cov(  
  object,  
  type = c("residual", "random", "all", "conditional", "marginal"),  
  aug = FALSE,  
  sparse = FALSE,  
  data = NULL  
)
```

Arguments

<code>object</code>	object which inherits class <code>lm</code> , <code>gls</code> or <code>lme</code>
<code>type</code>	“residual” for the variance-covariance for the residuals, “random” for the variance-covariance of the random effects or “all” for the sum of both.
<code>aug</code>	whether to augment the matrix of the random effects to the dimensions of the data
<code>sparse</code>	whether to return a sparse matrix (default is FALSE)
<code>data</code>	optional passing of ‘data’, probably needed when using this function inside other functions.

Details

Variance Covariance matrix for (non)linear mixed models

Value

It returns a `matrix` or a sparse matrix `Matrix`.

Note

See Chapter 5 of Pinheiro and Bates. This returns potentially a very large matrix of N x N, where N is the number of rows in the data.frame. The function `getVarCov` only works well for `lme` objects. The equivalence is more or less:

`getVarCov type = “random.effects”` equivalent to `var_cov type = “random”`.

`getVarCov type = “conditional”` equivalent to `var_cov type = “residual”`.

`getVarCov type = “marginal”` equivalent to `var_cov type = “all”`.

The difference is that `getVarCov` has an argument that specifies the individual for which the matrix is being retrieved and `var_cov` returns the full matrix only.

See Also

[getVarCov](#)

Examples

```
require(graphics)
require(nlme)
data(ChickWeight)
## First a linear model
f1m <- lm(weight ~ Time, data = ChickWeight)
v1m <- var_cov(f1m)
## First model with no modeling of the Variance-Covariance
fit0 <- gls(weight ~ Time, data = ChickWeight)
v0 <- var_cov(fit0)
## Only modeling the diagonal (weights)
fit1 <- gls(weight ~ Time, data = ChickWeight, weights = varPower())
v1 <- var_cov(fit1)
## Only the correlation structure is defined and there are no groups
fit2 <- gls(weight ~ Time, data = ChickWeight, correlation = corAR1())
```

```
v2 <- var_cov(fit2)
## The correlation structure is defined and there are groups present
fit3 <- gls(weight ~ Time, data = ChickWeight, correlation = corCAR1(form = ~ Time | Chick))
v3 <- var_cov(fit3)
## There are both weights and correlations
fit4 <- gls(weight ~ Time, data = ChickWeight,
             weights = varPower(),
             correlation = corCAR1(form = ~ Time | Chick))
v4 <- var_cov(fit4)
## Tip: you can visualize these matrices using
image(log(v4[,ncol(v4):1]))
```

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